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Fibonacci in Somos-5 by Complexification,
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Abstract

We use a complex seed for the Somos-5 sequence to get Gaussian integers with real and imaginary parts related by the Fibonacci sequence. For example, if $\{\mathbf{s}_n\}$ is Somos-5 with seed $(1, 1, \mathbf{i}, 1, 1)$, then $\{\mathbf{s}_{2n}\}_{n \geq 1}$ is the sequence

$1, 1, 1 + \mathbf{i}, 2 - \mathbf{i}, 2 + 3\mathbf{i}, 5 - 3\mathbf{i}, 5 + 8\mathbf{i}, 13 - 8\mathbf{i}, 13 + 21\mathbf{i}, 34 - 21\mathbf{i}, \dots$,
and the sequence of L_1 -norms is the Fibonacci sequence starting at 1.