

$$(21) \quad S_{k+1} = (4k^2 + 2k + 1)S_k + 2k(2k + 1)(4k^2 + 2k + 1)S_{k-1} \\ - 2k(2k + 1)(2k - 1)^2(2k - 2)^2S_{k-2} ,$$

valid for  $k = 0, 1, 2, \dots$ .



[Continued from page 168.]

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etc. Of course, that is (abstractly) the same thing we are doing in (2), (3).

In [7], Emma Lehmer examines the quadratic character of

$$\theta = (1 + \sqrt{5})/2 \pmod{p} .$$

If  $\theta$  is a quadratic residue of  $p$ , but not a higher power residue, then all quadratic residues can be generated by addition. In our construction,  $\theta$  is a primitive root and generates the quadratic nonresidues also.

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