

Assume

$$(5 + 3\sqrt{5})(9 + 4\sqrt{5})^t = s_t + L_{6t+2}5, \quad s_t^2 = 5L_{6t+2}^2 - 20.$$

$$(5 + 3\sqrt{5})(9 + 4\sqrt{5})^{t+1} = 9s_t + 20L_{6t+2} + \sqrt{5}(9L_{6t+2} + 4s_t)$$

$$9L_{6t+2} + 4s_t = 9L_{6t+2} + 4\sqrt{5}(\alpha^{6t+2} + \beta^{6t+2}) = 9L_{6t+2} + 20F_{6t+2}$$

$$\begin{aligned} L_{6t+8} &= \alpha^{6t+8} + \beta^{6t+8} = (9 + 4\sqrt{5})\alpha^{6t+2} + (9 - 4\sqrt{5})\beta^{6t+2} \\ &= 9L_{6t+2} + 20F_{6t+2}. \end{aligned}$$

(b) A second solution chain is given by the rational part (for  $s$ ) and the irrational part (for  $n$ ) of

$$(15 + 7\sqrt{5})(9 + 4\sqrt{5})^t, \quad t = 0, 1, 2, \dots$$

The proof that the irrational part of

$$(15 + 7\sqrt{5})(9 + 4\sqrt{5})^t$$

is identical to  $L_{6t+4}$  is similar to that used in III (a).

(c) A third solution chain is given by the rational part (for  $s$ ) and the irrational part (for  $n$ ) of

$$(40 + 18\sqrt{5})(9 + 4\sqrt{5})^t, \quad t = 0, 1, 2, \dots$$

The proof that the irrational part of

$$(40 + 18\sqrt{5})(9 + 4\sqrt{5})^t$$

is identical to  $L_{6t}$  is similar to that used in III (a).

Also solved by P. Bruckman, P. Tracy, and J. Ivie.

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$$y + 1 \leq z < y + (x/n)$$

is a necessary condition for a solution. Thus, we see that there can be no solution for integer  $x$ ,  $1 \leq x \leq n$ , a well known result (see [1, p. 744]). Again, if  $y = n$ , there is no solution for  $1 \leq x \leq n$ , a well known result (see [1, p. 744]). Our proof can also be used to establish the following general result.

*Theorem 2.* For  $n \geq m \geq 2$  and integers  $A \geq 1$ ,  $B \geq 1$ , the equation

$$Ax^n + By^m = Bz^m$$

has no solution whenever  $Ax^{n-m+1} + Bmy \leq Bmz$ .

REMARK. Theorem 2 gives Theorem 1 for  $A = B$  and  $n = m$ .

#### REFERENCE

1. L.E. Dickson, *History of the Theory of Numbers*, Vol. 2, Diophantine Analysis, Carnegie Institute of Washington, 1919, Reprint by Chelsea, 1952.

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