$$\sum_{n=1}^{\infty} \frac{(-1)^{n(k+1)}}{F_n F_{n+1} \cdots F_{n+2k+1}} = \frac{1}{(F)_{2k}} \sum_{j=0}^{2k} (-1)^{\frac{1}{2}j(j+1)-jk} \begin{cases} 2k \\ j \end{cases} A_{2k-j+1}$$
(6.7)  

$$- \frac{1}{(F)_{2k}} \sum_{j=0}^{2k} (-1)^{\frac{1}{2}j(j+1)-jk} \begin{cases} 2k \\ j \end{cases}$$

$$\cdot \sum_{n=1}^{j} \frac{(-1)^n}{F_n F_{n+2k-j+1}} ,$$

where now  $\begin{cases} 2k \\ j \end{cases}$  and  $A_{2k-j+1}$  are expressed in terms of Fibonacci numbers.

## REFERENCE

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 $\rho = 1$  stems from its application to the partitioning of integers into distinct Fibonacci numbers. These applications are investigated in the papers listed in References. When  $\rho$  is a root of unity, series (1) again has partition — theoretic congruence which we exploited to some extent in Section 5.

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