

¹ A Simple Way to Improve the Diurnal Cycle in ² Convective Rainfall over Land in Climate Models

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Abstract.

The diurnal cycle in convective rainfall over land usually peaks in the late afternoon. In most climate models, the diurnal peak in convective rainfall occurs several hours too early, and is often near local solar noon. We argue that this bias originates from the methods used in convective parameterizations to calculate the cloud base mass flux. In most convective parameterizations, the initial convective mass flux is determined from the Convective Available Potential Energy (CAPE) of a thin layer near the surface. Near surface CAPE increases rapidly during the morning when there is an increase in the upward flux of heat and water vapor. However, the mass weighted CAPE of the boundary layer as a whole responds much more slowly to the increase in downward solar radiation at the surface. Using a recently developed convective parameterization in version 4 of the Community Atmosphere Model (CAM4), we show that the overall accuracy in the diurnal simulation of convective precipitation increases as the number of near surface layers from which convective air parcels are permitted to originate increases from one to four.

1. Introduction

19 Most of the rainfall in the tropics, and in mid-latitudes during the summer months,
20 originates from convective clouds. Convective rainfall over land exhibits a strong diur-
21 nal cycle, with a characteristic peak in the late afternoon or early evening [*Nesbitt and*
22 *Zipser, 2003*]. This diurnal cycle has a wide range of impacts on climate forcings, sur-
23 face energy and water budgets, regional circulation patterns, and atmospheric chemistry.
24 For example, the diurnal cycle in convective rainfall gives rise to diurnal cycles in cloud
25 amount [*May et al., 2012*] and relative humidity which modify the propagation of solar
26 and thermal radiation through the troposphere and affect the surface radiation balance.
27 Regional scale sea breeze circulations, especially in the tropics, are usually driven by the
28 diurnal variation in convective rainfall [*Ploshay and Lau, 2010*]. The diurnal cycle in the
29 convective transport of chemical tracers from the boundary layer to the free troposphere
30 will give rise to diurnal cycles in the free tropospheric mixing ratios of most chemical
31 tracers. And for chemical tracers such as carbon dioxide which also exhibit strong diurnal
32 cycles in the boundary layer [*de Arellano et al., 2004*], the net convective transport of the
33 chemical species from the boundary layer will depend on the phase relationship between
34 the two diurnal cycles.

35 Unfortunately, the diurnal cycle in convective rainfall over land is poorly represented
36 in many climate [*Dai, 2006*] and weather forecast [*Betts and Jakob, 2002; Clark et al.,*
37 *2007*] models. In many models, the diurnal peak in convective rainfall occurs several hours
38 too early, and is often near local solar noon [*Dai, 2006; Bechtold et al., 2004*]. This bias
39 in the diurnal timing of convective rainfall will generate errors in the reflection of solar

40 radiation back to space, especially by extensive upper tropospheric cirrus anvil clouds
41 [*Taylor, 2012*], and is the dominant source of error in forecasts of tropical rainfall over
42 land on short timescales [*Chakraborty, 2010*].

43 The absorption of solar energy by the land surface increases the upward flux of heat and
44 water vapor, and increases the fraction of near surface air parcels with positive Convec-
45 tive Available Potential Energy (CAPE). The existence of near surface air with positive
46 CAPE is a thermodynamic precondition for moist convection. In many convective pa-
47 rameterizations, the convective cloud base mass flux is directly related to the CAPE of
48 a single model layer which is usually the model layer closest to the surface [*Grell, 1993*;
49 *Jakob and Siebesma, 2003*; *Bechtold et al., 2001*]. However, even when near surface CAPE
50 is present, there are many physical mechanisms which can delay the onset of convective
51 precipitation. For example, it is likely that deep convective plumes entrain air not only
52 from the shallow surface layer, but from the entire boundary layer. In this case, the mass
53 weighted CAPE of the boundary layer as a whole may be a better proxy for the convective
54 cloud base mass flux than the CAPE of the near surface layer. We refer to the lag in the
55 development of convective precipitation associated with the deepening of the convective
56 layer as boundary layer resistance.

57 There are a variety of microphysical processes that contribute to delays in the devel-
58 opment of convective precipitation. These include timescales associated with warm rain
59 processes and the timescale required for convective plumes to rise sufficiently high that the
60 ambient temperature is cold enough to initiate the activation of ice condensation nuclei.

61 The entrainment of subsaturated air from the background atmosphere into convective
62 plumes can also be expected to delay the onset of convective precipitation. Entrainment

63 is associated with condensate evaporation, cooling, and loss of buoyancy. Due to mixing,
64 most convective plumes dissipate before producing precipitation. However, by moistening
65 the local atmosphere, they diminish the impact of entrainment on the development of
66 subsequent plumes. There can therefore be an additional delay in the onset of deep
67 convection, equal to the timescale over which shallow convection increases the mid-level
68 relative humidity to the threshold required to support deep convection [*Tompkins, 2001a*].

69 Convective precipitation often occurs in association with some form of mesoscale orga-
70 nization such as squall lines [*Tulich and Kiladis, 2012*]. In this case, the development of
71 convective precipitation can be expected to be delayed by processes associated with the
72 development of the precipitating stratiform anvil, the formation of evaporatively driven
73 downdrafts, and the horizontal propagation of the cold pools and gust fronts that pro-
74 vide the vertical uplift necessary to overcome convective inhibition and rapidly convert
75 positive CAPE air near the surface into buoyant air within convective plumes.

76 Finally, at some locations, convection is associated with propagating convective systems
77 that have been remotely generated by, for example, orography [*Ahijevych et al., 2004*].
78 In this case, there would be an additional delay associated with the movement of the
79 convective system from its place of origin.

80 Although there are numerous mechanisms which can delay the onset of convective rain-
81 fall over land, we show that the representation of the diurnal cycle in convective rainfall
82 over land in a climate model can be substantially improved by a more accurate treatment
83 of boundary layer resistance. Within each grid column, rather than restrict the initiation
84 of convective updrafts to the model layer nearest the surface, we test for positive CAPE in
85 each of the four lowest model layers. The initial convective mass flux therefore responds

86 to the convective instability of the column as a whole, rather than to the CAPE of a
87 relatively thin layer near the surface. This modification delays the onset of convective
88 rainfall over land, and brings the diurnal rainfall peak in most regions into much better
89 agreement with observations.

90 The method outlined here for improving the diurnal cycle in convective rainfall over
91 land is quite simple, and should be relatively easy to implement in most climate models.
92 However, there have been several other recent studies discussing ways in which the rep-
93 resentation of the diurnal cycle in convective rainfall over land can be improved. Some
94 models show improvement with increased horizontal resolution [*Sato et al.*, 2009; *Ploshay*
95 *and Lau*, 2010; *Yamada et al.*, 2012], use of different convective parameterizations [*Liang*
96 *et al.*, 2004], or changes in the triggering scheme [*Zhang*, 2003; *Xie et al.*, 2004].

97 Other climate models have demonstrated improvement in the diurnal cycle by incorpo-
98 rating some representation of convective organization into convective parameterizations.
99 Organized mesoscale convective systems contribute to the nonlinear intensification of con-
100 vective precipitation through the formation of cold pools which provide a dynamical mech-
101 anism for rapidly overcoming convective inhibition [*Tompkins*, 2001b; *Khairoutdinov and*
102 *Randall*, 2006]. However, most climate models employ convective parameterizations that
103 interact with the background atmosphere in a fixed manner. Convective organization
104 can be introduced into convective parameterizations by using a variable from the local
105 grid column, or output of the convective parameterization from the previous timestep,
106 to modify the behaviour of the convective parameterization during the current timestep.
107 Convective organization variables have included the height of the lifting condensation
108 level [*Stratton and Stirling*, 2012], the existence of surface cold pools [*Rio et al.*, 2009],

109 and column evaporation [Mapes and Neale, 2011]. These approaches have also had some
110 success in delaying the onset of convective precipitation over land, and generating more
111 realistic diurnal cycles [Stratton and Stirling, 2012; Rio et al., 2009].

2. Datasets

112 There is significant geographic variability in the diurnal cycle of convective rainfall
113 over land [Yang and Slingo, 2001]. Here, we use the Tropical Rainfall Measuring Mis-
114 sion (TRMM) 3B42 gridded rainfall dataset [Liu et al., 2012] to determine the regional
115 variability in the monthly mean diurnal cycle of convective rainfall. This dataset has a
116 temporal resolution of 3 hours and a spatial resolution of 0.25° . We use TRMM 3B42 rain
117 rates from 2003 to 2010 to calculate the mean diurnal cycle in rainfall within every CAM4
118 grid cell. For each land grid cell in which there is significant convective precipitation, we
119 calculate the correlation coefficient between the TRMM diurnal cycle and the diurnal cy-
120 cles of various CAM4 model simulations. The global average of this correlation coefficient
121 is then used as an objective indicator of the fidelity with which the model matches the
122 observed diurnal cycle.

123 It is desirable that climate model improvements in the diurnal cycle of convective pre-
124 cipitation not compromise the climatological rainfall patterns generated by a model. We
125 therefore use monthly mean rainfall data on a 2.5° by 2.5° grid from the Monthly Precip-
126 itation Analysis (1979-Present) of the Global Precipitation Climatology Project (GPCP)
127 [Adler et al., 2003] to determine the accuracy of the climatological rainfall patterns gen-
128 erated by the CAM4-IF model.

3. Overview of the Convective Parameterization

129 The model simulations discussed in this paper are based on an implementation of a
130 recently developed convective parameterization [Folkins, 2009] in version 4 of the Com-
131 munity Atmosphere Model (CAM4). During implementation, this parameterization was
132 also modified to include a representation of subgridscale convective organization. One
133 of the benefits of introducing convective organization is that it enabled the parameter-
134 ization to exhibit a wider range of convective responses, and permitted the removal of
135 parameterizations for both shallow [Hack, 1994] and deep [Zhang and McFarlane, 1995]
136 convection from the default version of CAM4, and their replacement by a single convective
137 parameterization.

138 There have been several changes to the convective parameterization since the initial
139 publication [Folkins, 2009]. Most of these changes are related to the introduction of
140 convective organization. These changes do not have a strong impact on the diurnal cycle,
141 and are therefore discussed in the Appendix.

142 The convective parameterization is a mass flux scheme in which the effects of convective
143 updrafts and downdrafts on the background atmosphere are represented by a spectrum
144 of updraft and downdraft parcels moving vertically under the influence of buoyancy. The
145 updraft parcels originate from the four model levels closest to the surface. These levels
146 occur at roughly 980, 958, 918, and 856 hPa, corresponding to pressure thicknesses of
147 14.5, 29.3, 53.0, and 72.7 hPa respectively. At each of the four levels nearest the surface,
148 we assume that subgridscale variability in temperature and relative humidity gives rise to
149 a moist enthalpy spectrum. The width of this spectrum is an increasing function of the
150 recent rainfall within the grid column. This enthalpy spectrum is then used to define a

151 parcel spectrum within each near surface layer, with each parcel having the same mass per
152 unit area. The CAPE of each parcel is evaluated independently. If it exceeds 20 J/kg, the
153 parcel is given an initial upward kinetic energy of 20 J. The parcel then moves vertically
154 under the influence of buoyancy using specified rules for precipitation formation and mass
155 exchange with the background atmosphere. When the buoyancy of the parcel becomes
156 negative, it fully detrains into the background atmosphere.

157 Updraft parcels produce two kinds of precipitation. If the temperature of an updraft
158 parcel is higher than T_{freeze} (here $T_{freeze} = 253$ K), and the updraft parcel condensate
159 loading exceeds a prescribed threshold, it produces updraft rain. This form of precipi-
160 tation is assumed to remain within the cloud at all heights and does not evaporate. At
161 temperatures colder than T_{freeze} , the updraft parcels produce updraft snow. This form of
162 precipitation is assumed to remain within cloud until the melting level, at which point it
163 exits cloud base, melts, and starts to evaporate and generate downdrafts.

164 In the model, the induced gridscale subsidence within a convecting grid column tends
165 to produce positive geopotential height anomalies, and divergent outflow, in the upper
166 troposphere. The upward gridscale motions required to balance this divergent outflow
167 increase the relative humidity of the mid and upper troposphere. In this case, water
168 vapor in excess of 90 % relative humidity with respect to ice within any grid box above
169 the melting level is converted to stratiform snow. This stratiform snow is then added to
170 the updraft snow and treated in an identical manner.

171 In convective regions, the upper part of the boundary layer also tends to become
172 supersaturated. Below 750 hPa, we remove moisture in excess of 90 % relative humidity

173 with a two hour timescale. The rain generated by this stratiform mechanism is added to
174 the updraft rain, and treated in an identical manner.

175 Figure 1 gives a conceptual overview of the procedure used to generate downdrafts.
176 The total snow, from both updraft and stratiform sources, is equally divided into three
177 shafts. The three shafts are assigned lengths of 9 km, 20 km, and 45 km. The fraction of
178 the grid column occupied by each shaft is calculated from the assumption that the local
179 precipitation rate within each shaft is 100 mm/day. Each snow shaft is divided into 15
180 layers. A descending snow layer encounters cloud free air at the first model level having
181 a temperature above 0 °C. As the layers sequentially descend through each model level,
182 they melt within, and evaporate into, air parcels whose fractional area is equal to the
183 fractional area of the parent snow shaft. The exposure time of a particular air parcel
184 to a snow (rain) layer is determined in part from the remaining width of the layer and
185 its prescribed fall speed. In general, the negative buoyancy of an air parcel will increase
186 with the passage of every additional snow (rain) layer. When the negative buoyancy of an
187 air parcel is sufficiently large to overcome the stability of the atmosphere, the downdraft
188 parcel descends one model level. Due to interactions with multiple snow (rain) layers of
189 a single snow shaft, an air parcel may descend multiple model levels within a timestep,
190 and successively descend toward, and sometimes detrain at, the surface. This is more
191 likely to occur for air parcels under the taller snow shafts, which have thicker snow (rain)
192 layers, longer exposure times, and generate more intense cooling. The fall speed of the
193 snow (rain) layers is parameterized in terms of temperature (as a surrogate for density),
194 and typically decreases from 8 m/s just below the melting level to 5 m/s near the surface.
195 No allowance is made for the slower fall speeds of snowflakes prior to melting.

196 The moist enthalpy (k_m), total water mixing ratio (r_t), and dry mass (m_d) of the updraft
197 and downdraft parcels are updated as the parcels move vertically, mix, precipitate, and
198 extract water from falling precipitation. Entrainment of updraft and downdraft parcels
199 from the background atmosphere generates local sinks of k_m , r_t , and m_d , whereas parcel
200 detrainment generates sources of conserved quantities. It is assumed that the convective
201 parameterization does not change the top and bottom pressure levels of each grid box, and
202 that the difference between the top and bottom pressure is related to the mass of a grid
203 box via hydrostatic balance. At levels where the detrainment of mass exceeds entrainment,
204 the grid box mass will exceed the hydrostatic mass (and conversely, where entrainment
205 exceeds detrainment). To restore hydrostatic balance, the model moves mass vertically.
206 For example, deep convection is typically associated with net mass detrainment at upper
207 levels, and therefore triggers immediate downward subsidence within the grid column.
208 Net upward vertical motion associated with the convective (sub-gridscale) movement of
209 updraft and downdraft parcels is therefore usually associated with column heating.

210 The default CAM4 model, and the version of the model with the new convective pa-
211 rameterization (CAM4-IF), were run with a horizontal resolution of $1.9^\circ \times 2.5^\circ$ (latitude
212 \times longitude), 26 vertical levels, and a timestep of 30 minutes. The model runs start on
213 January 1, 2000 and end on December 31, 2002, using fixed climatological sea surface
214 temperatures [Gent *et al.*, 2011]. The initial atmospheric state was a climatological state
215 for the start date from the CAM4 model.

4. Results

216 Figure 2 shows the diurnal cycle in precipitation over land simulated by the CAM4 and
217 CAM4-IF model runs, together with the observed diurnal cycle from the TRMM 3B42

218 gridded rainfall dataset. We selected four areas for comparison: the Southeast United
219 States, Equatorial Brazil, Equatorial Africa, and Northern India. The boundaries of each
220 region are shown in Figure 3. For simplicity, we chose areas that had weak orography.
221 For each region, we also selected months in which there was enhanced rainfall. In all four
222 regions, the precipitation of the default CAM4 model peaks near solar noon, a feature
223 common to many climate models [Bechtold *et al.*, 2004; Dai and Trenberth, 2004]. The
224 CAM4-IF model accurately simulates the timing of the late afternoon diurnal rainfall
225 maximum in all four regions. Both models tend to overestimate the rainfall rate in the
226 Equatorial Africa and Northern India regions.

227 The diurnal rainfall plots shown in Figure 2 suggest that the CAM4-IF model reproduces
228 the diurnal variation in convective rainfall much more accurately than the default CAM4
229 model. However, it would be desirable to be able to identify the geographic regions where
230 the CAM4-IF model fails to reproduce the diurnal cycle in convective rainfall, and to have
231 an objective measure of the overall ability of the CAM4-IF model to simulate the diurnal
232 cycle. The TRMM 3B42 rainfall rates were therefore first averaged to produce a new
233 rainfall dataset having the same $1.9^\circ \times 2.5^\circ$ horizontal resolution as the CAM4 model
234 grid. We then calculated the mean diurnal variation at each grid cell for every month,
235 using TRMM rain rates from 2003 to 2010. The three years of rainfall data from the
236 CAM4-IF model run were then used to calculate the average rain rate at the eight daily
237 TRMM times. We then calculated, for each month, the correlation coefficient between the
238 eight local TRMM and CAM4-IF diurnal rain rates. This was done only at land grid cells
239 where both the TRMM and CAM4-IF monthly mean rain rates exceeded 2 mm/day, and
240 at locations where the rainfall could be assumed to be convective. This was considered

241 to be 20 °S - 20 °N, 40 °S - 20 °S during December - February, and 20 °N - 40 °N during
242 June - August. Figure 3 shows the geographic distribution of the correlation coefficient,
243 averaged over the months in which the above two conditions were satisfied. Grid cells
244 shown in blue indicate regions where the shape of the local diurnal cycle in convective
245 rainfall is accurately simulated by the CAM4-IF model. This includes most of Australia,
246 the maritime continent, India, the Southeast United States, Central America, and parts
247 of South America. The diurnal cycle is poorly simulated in Equatorial Africa, parts of
248 China and South America, and the Midwestern United States.

249 At a given grid cell, there can be a variety of reasons why the local diurnal cycle in
250 convective rainfall is poorly simulated by the CAM4-IF model. In general, however, the
251 simulation of the local diurnal cycle in convective rainfall is poor when the local peak
252 in convective rainfall does not occur in the late afternoon or early evening. In Figure
253 4, the local correlation coefficient between the CAM4-IF and TRMM diurnal cycles of
254 a particular month is plotted against the time of the local peak in TRMM rainfall. We
255 also plot the mean variation of the correlation coefficient against the local solar time of
256 the TRMM rainfall maximum. The correlation coefficient is largest when the observed
257 rainfall peak occurs between local solar noon and midnight. At other times, the correlation
258 between the two diurnal cycles is near zero.

259 The dashed line of the upper panel of Figure 4 shows the variation in the frequency
260 of occurrence of the local solar time of the TRMM diurnal rainfall maximum, at grid
261 cells where the rainfall is considered to be convective. There is a peak in the occurrence
262 of largest rainfall rates in the late afternoon. In roughly a quarter of all convective grid
263 cells, the local peak in convective rainfall occurs between 16:00 and 17:00. The solid curve

264 in the upper panel of Figure 4 shows the frequency of occurrence of peak rainfall in the
265 CAM4-IF model. The overall shape is similar to the observed frequency of occurrence.
266 However, the peak of the CAM4-IF curve occurs 1 hour earlier than the observed peak,
267 indicating that peak rainfall in the CAM4-IF model continues to occur somewhat earlier
268 than observed.

269 It should be noted that the 3 hour time resolution of the TRMM 3B42 dataset will give
270 rise to an error in the time of the diurnal rainfall maximum at any given grid cell of about
271 an hour. However, if these errors are randomly distributed, the error in the global mean
272 estimate of the diurnal rainfall maximum from this error source should be less than an
273 hour. The difference shown in Figure 4 in the timing of the most common diurnal rainfall
274 maximum is therefore likely to be significant.

275 The upper panel of Figure 3 shows the geographic distribution of the local solar time
276 of peak TRMM rainfall, for the month with highest rainfall. The peak in diurnal rainfall
277 occurs at a nonstandard time for grid cells shown in dark blue (near midnight), and red
278 and yellow (overnight). This occurs in the Sahel (e.g. Africa near 10 °N), the Himalayas,
279 parts of Northern Australia, Argentina, the Andes, and the Midwestern United States.
280 Many of these regions are mountainous or semi-arid, and correspond to regions of reduced
281 correlation in the lower panel. In particular, the upper panel of Figure 3 shows that South
282 America exhibits three nearly parallel diagonal lines of anomalous rainfall timing, one of
283 which corresponds to the Andes. Each of these diagonal lines is associated with a similar
284 line of reduced correlation in the lower figure.

285 Many of the regional anomalies in the diurnal timing of convective rainfall shown in the
286 upper panel of Figure 3 have been previously discussed, and variously attributed to local

287 changes in the genesis, propagation, or organization of convective systems. For example,
288 the nighttime peak over the Great Plains of the United States has been attributed to the
289 eastward propagation of mesoscale convective systems originating during the afternoon
290 over the Rocky Mountains [*Dai et al.*, 1999; *Ahijevych et al.*, 2004]. Along the northeast
291 coast of Brazil, the nocturnal maximum during January - April has been attributed to a
292 convergence zone forming near the coast between the onshore northeasterly trade winds
293 and an offshore land breeze, with squall lines form along the convergence zone often
294 propagating inland [*Kousky*, 1980; *Cohen et al.*, 1995]. The middle line of maximum
295 nighttime rainfall across Brazil appears similar to a feature that was previously tentatively
296 attributed to a remote response to diurnally forced convection over the Andes [*Garreaud*
297 *and Wallace*, 1997]. The region of anomalous diurnal timing in Northern Argentina and
298 Paraguay corresponds to a preferred region for the development of mesoscale convective
299 complexes [*Velasco and Fritsch*, 1987; *Salio et al.*, 2007]. Many of these features are
300 presumably challenging to simulate in a climate model of this spatial resolution. Some
301 of the features of the diurnal cycle in South American convective precipitation have been
302 simulated by a regional scale model with 50 km resolution [*da Rocha et al.*, 2009]. Over
303 the United States, there was a mixed improvement in the simulation of the diurnal cycle
304 when the horizontal grid size was decreased from 2 ° to 0.5 ° [*Lee et al.*, 2007].

305 It is not possible to isolate a single reason for the improvement in the diurnal cycle
306 of convective rainfall in going from the default CAM4 model to the CAM4-IF model.
307 However, the majority of the improvement appears to result from a change in the mass
308 flux closure. Prior to deep convection, the default CAM4 model first identifies the layer
309 near the surface with the largest moist static energy. This is usually the layer closest to the

310 surface. If the CAPE of this layer exceeds a threshold of 70 J/kg, mass is removed from the
311 layer with a 1 hour timescale and entrained into a convective plume, which subsequently
312 rises within the grid column. The CAM4-IF model, on the other hand, calculates the
313 CAPE of the bottom four model layers. If the CAPE of any layer exceeds a threshold of
314 20 J/kg, mass from the layer is used to construct an updraft parcel spectrum as described
315 in the Appendix. In this method, the total initial updraft parcel mass roughly scales with
316 the CAPE of the boundary layer as a whole, rather than the CAPE of a relatively thin
317 layer near the surface. This difference can affect the diurnal variation in convective rainfall
318 generated by the two methods. Figure 5 shows the diurnal variation in the CAPE of the
319 near surface layer of the CAM4-IF model, and of the average mass weighted CAPE of the
320 lowest four model layers, both averaged over the Southeast United States region in July.
321 The CAPE of the near surface layer sharply increases after sunrise and peaks near 11:00.
322 The secondary peak near 20:00 is caused by an early evening local increase in water vapor
323 mass mixing ratio. The mass weighted CAPE of the boundary layer responds much more
324 slowly to the morning increase in solar insolation and reaches a maximum near 14:00.

325 To investigate the effect of changes in the mass flux closure on the diurnal cycle of
326 convective rainfall, we ran five additional simulations of the CAM4-IF model. In the
327 LEV1, LEV2, and LEV3 simulations, updraft parcels were entrained from the lowest
328 one, two, and three model levels respectively. To compensate for the reduction in the
329 number of pressure levels contributing to the updraft mass flux, the convective removal
330 timescale t_{remove} was reduced to 2 (LEV1), 4 (LEV2), and 8 (LEV3) hours. We also wanted
331 to investigate the degree to which the implementation of subgridscale organization was
332 affecting the simulation of the diurnal cycle. We therefore ran two additional simulations.

333 In the NO-ORG simulation, all five organization variables were fixed at constant values.
334 This includes (with the fixed value in brackets) the mass flux amplification factor AMP (3),
335 the updraft parcel spectrum width dk_m (1500 J/kg), the buoyancy mixing scale b_{mix} (0.18
336 m/s²), the maximum updraft condensate $r_{l,max}$ (1.6 g H₂O/kg dry air), and the updraft
337 condensate to precipitation conversion efficiency f_{precip} (0.5). In a second simulation called
338 NO-AMP, the mass flux amplification factor was fixed as given above, but the other four
339 organization parameters varied as described in the Appendix.

340 For each of the five additional simulations, we calculated the local correlation coefficient
341 between the TRMM and simulated diurnal cycles at grid cells considered to be convective,
342 using the definition discussed previously. In Figure 6, we show the variation in the average
343 value of the correlation coefficient between the model runs. The diurnal variation in
344 convective rainfall was most poorly simulated by the default CAM4 model run, which
345 exhibited an overall anticorrelation with TRMM rainfall on diurnal timescales. For the
346 CAM4-IF model, there was a progressive improvement in the simulation of the diurnal
347 cycle as additional near surface layers were permitted to generate convective updraft
348 parcels. The additional of subgridscale convective organization was also associated with a
349 modest improvement in the simulation of the diurnal cycle, with the average correlation
350 coefficient of the CAM4-IF model run slightly higher than the coefficients of both NO-
351 AMP and NO-ORG model runs.

352 New implementations of convective parameterizations in climate models are tested
353 against a large number of metrics in addition to the diurnal cycle. These include cli-
354 matological rainfall patterns, relative humidity and temperature profiles, conservation
355 properties, computational efficiency, transport properties, and sources of rainfall variance

356 such as hurricanes, equatorially trapped convectively coupled waves, and the Madden
357 Julian Oscillation. It is desirable that increased agreement in one metric not be offset
358 by decreased agreement in others. Space considerations preclude a full discussion of the
359 performance of the CAM4-IF model. In our experience, however, allowing convective up-
360 draft parcels to originate from the lowest four model layers (as opposed to just the near
361 surface layer) does not undermine other aspects of the CAM4-IF model. In particular,
362 the accuracy of the climatological rainfall distribution of the CAM4-IF model is compa-
363 rable to that of the default CAM4 model. For each month, for all convective grid cells,
364 we calculated the correlation coefficient between the monthly mean rain rates of the two
365 models and monthly mean GPCP rainfall. Figure 7 shows the seasonal variation of this
366 correlation for the ocean and land grid cells. During Northern Hemisphere Fall, the cli-
367 matological distribution of convective rainfall over the ocean is simulated more accurately
368 by the default CAM4 model. Otherwise, the correlation coefficients of the CAM4 and
369 CAM4-IF models are similar to each other.

5. Summary

370 Most of the convective parameterizations used in climate models are mass flux based pa-
371 rameterizations in which the effects of convective clouds on the background atmosphere are
372 represented by updraft plumes or parcels moving upward under the influence of buoyancy.
373 In many convective parameterizations, the updraft plume or parcel is usually entrained
374 from the model level with the highest moist static energy, or a relatively thin surface
375 layer [Grell, 1993; Jakob and Siebesma, 2003; Bechtold et al., 2001]. However, there is
376 no reason, other than computational expediency, to restrict the initiation of convective
377 clouds exclusively to a single layer near the surface. Over the tropical oceans, the positive

378 CAPE surface layer typically extends to 880 hPa, while over Southeast United States, the
379 positive CAPE layer typically extends to 840 hPa [*Mitovski et al.*, 2013]. In the default
380 CAM4 model, due to the practice of restricting the initiation of convective plumes to the
381 layer with highest moist static energy, convective plumes usually originate from a near
382 surface layer that has a pressure thickness of about 14.5 hPa. In this case, in order to
383 generate realistic deep convective mass fluxes, it is necessary that the convective removal
384 timescale from this layer be very short (1 hour).

385 The rapid removal of positive CAPE air from a thin surface layer generates a bias in
386 the simulation of the diurnal cycle. Over land during the day, boundary layer turbulence
387 gives rise to an upward flux of heat and water vapor from the earth's surface. This upward
388 transport helps generate air parcels with positive CAPE throughout the boundary layer.
389 However, due to the gradual increase in the height of the boundary layer during the day,
390 the diurnal cycle in CAPE is altitude dependent, with CAPE in the upper part of the
391 boundary layer exhibiting a more strongly lagged response to increases in solar insolation.
392 As a result, the mass weighted CAPE of the boundary layer exhibits a peak at in the
393 late afternoon. The timing of this peak is roughly in phase with the diurnal cycle in
394 convective rainfall over land in most regions. Climate models should therefore be able to
395 generate a reasonable cycle in convective rainfall over land, provided they use convective
396 parameterizations which employ CAPE based mass flux closures which are sensitive to
397 the convective instability of the grid column as a whole, rather than simply a thin surface
398 layer. Here, we have shown that the CAM4-IF model exhibits a significant improvement
399 in the simulation of the diurnal cycle in convective rainfall over land, as the number of
400 near surface levels used to generate convective air parcels increases from one to four.

401 The method outlined here for generating the late afternoon peak in convective rainfall
402 over land is quite simple, and seems to be the most natural explanation from an energetic
403 point of view. However, there are numerous other physical mechanisms that can affect
404 the timing of the diurnal peak in convective rainfall. In particular, there are many regions
405 where the diurnal peak in convective rainfall occurs at night. Most of the rainfall in
406 these regions appears to be associated with organized convective systems that are either
407 remotely generated, or are associated with local synoptic forcings that favour nighttime
408 development. In these regions, the correlation between the local diurnal cycle simulated
409 by the CAM4-IF model and the observed diurnal cycle measured by TRMM is only weakly
410 positive. Further improvement in the simulation of the diurnal cycle in convective rainfall
411 over land by the CAM4-IF model will therefore require more realistic simulations of the
412 types of convective organization that generate peak rainfall rates during the evening.

Appendix A: Subgridscale Convective Organization in the CAM4-IF Model

413 The one dimensional behaviour of the convective parameterization used in the CAM4-
414 IF model has been described previously [*Folkins, 2009*]. However, during implementation
415 in the CAM4 model, the parameterization was modified to include a form of subgridscale
416 organization. Rather than being fixed at constant values, five of the model parameters
417 depend on the precipitation rate generated by the model grid column over the past sev-
418 eral hours. Although the introduction of convective organization results in only a modest
419 improvement in the simulation of the diurnal cycle in convective rainfall over land, it
420 does have a number of significant benefits. Due to convective organization, the convective
421 parameterization generates a wider range of cloud types, and permits both the shallow
422 [*Hack, 1994*] and deep [*Zhang and McFarlane, 1995*] convective schemes of the default
423 CAM4 model to be replaced by a single convective parameterization. It also gives rise to
424 more rapid and realistic growth and decay rates of convective precipitation, a continuous
425 growth in the mean height of divergent outflow from shallow to deep during the devel-
426 opment of high rain events, and a boundary layer cooling coincident with high rain rates
427 that is roughly consistent with the observed cooling [*Mitovski et al., 2010*].

A1. Boundary Layer Moist Enthalpy Spectrum

428 The variability in boundary layer temperature and specific humidity increase when
429 convective precipitation is present [*Zhang and Klein, 2010*]. During deep convection, in
430 cloud resolving simulations, the moist static energy of parcels recently heated by the
431 surface can exceed the moist static energy of downdraft parcels by as much as 10 kJ/kg
432 [*Khairoutdinov and Randall, 2006*]. Therefore, at each of the four model levels closest to
433 the surface, we define a moist enthalpy spectrum whose width dk_m is an increasing function

434 of the recent convective precipitation of the local grid column. The center of each moist
 435 enthalpy spectrum is equal to the moist enthalpy of the grid box. The enthalpy spectrum
 436 is used to define an updraft parcel spectrum, with each parcel having equal mass.

437 To define the width of the moist enthalpy spectrum, we first define a precipitation rate
 438 that is roughly equal to the local mean rate over the last several model timesteps.

$$439 \quad R_{mean} = \left(1 - \frac{t_{step}}{\tau_{org}}\right) R_{mean,prev} + \frac{t_{step}}{\tau_{org}} R_{current} \quad (A1)$$

440 In this expression, t_{step} is the timestep of the CAM4 model (30 minutes), τ_{org} is a timescale
 441 over which R_{mean} responds to changes in precipitation ($\tau_{org} = 2$ hours), $R_{mean,prev}$ is the
 442 previous local value of the mean precipitation rate, and $R_{current}$ is the current precipita-
 443 tion rate in the grid column. With this definition, R_{mean} is roughly equal to the mean
 444 precipitation rate of the local grid column over the time interval τ_{org} . It would be possi-
 445 ble to simply set R_{mean} equal to the precipitation at the most recent timestep by using
 446 $\tau_{org} = t_{step}$. However, this tends to introduce excessive noise into the rainfall rate gener-
 447 ated by the model. The convective organization variables therefore respond in a lagged
 448 manner to changes in local rainfall.

449 The width of the moist enthalpy spectrum is then defined using the following sigmoidal
 450 expression.

$$451 \quad dk_m = dk_{m,min} + \frac{dk_{m,max}}{1 + e^{-R_{norm}}} \quad (A2)$$

452 $dk_{m,min}$ is a minimum width of the enthalpy spectrum, $dk_{m,min} + dk_{m,max}$ is the maximum
 453 width, and R_{norm} is defined in terms of R_{mean} and two additional rainfall parameters R_{half}
 454 and R_{scale} .

$$455 \quad R_{norm} = \frac{R_{mean} - R_{half}}{R_{scale}} \quad (A3)$$

456 R_{half} is the rain rate at which the spectrum width is roughly equal to half its maximum
 457 value. R_{scale} is a parameter that determines the steepness of the sigmoidal curve. For small
 458 R_{scale} , the sigmoidal function approaches a step function. Figure 8 shows the dependence
 459 of dk_m on R_{mean} obtained by using the above three equations, and the parameter values
 460 given in Table 1.

461 If the convective precipitation within a grid column increases, the sigmoidal expression
 462 for dk_m will increase the value of dk_m parameter on the next timestep. This increase
 463 in boundary layer variance will increase the fraction of the boundary layer mass with
 464 positive CAPE, and contribute to a further increase in convective precipitation. The
 465 introduction of the dk_m parameter therefore contributes to a nonlinear intensification of
 466 high rain events, and an increase in the overall rainfall variance. It should also be noted
 467 that the downdraft formulation of the model is constructed to enable the direct injection
 468 of downdraft parcels with reduced moist static energy into the boundary layer. Without
 469 the introduction of a moist enthalpy spectrum, this direct injection of cold air would be
 470 a strong negative feedback on the development of high rain events in the model.

A2. Cloud Base Mass Flux

At each of the four lowest model levels, we define an initial updraft parcel mass per unit area spectrum $m_{p,i}$ (where i ranges from 1 to N) using the following expression.

$$m_{p,i} = \text{AMP} \left(\frac{t_{\text{step}}}{t_{\text{remove}}} \right) \left(\frac{\text{cape}(i)}{\text{cape}_{\text{scale}}} \right) \left(\frac{dp}{gN} \right). \quad (\text{A4})$$

Here, dp refers to the difference between the top and bottom pressures of the layer, $\text{cape}(i)$ to the CAPE of parcel i within the enthalpy spectrum, $\text{cape}_{\text{scale}}$ is a parameter (1000 J/kg), t_{remove} a CAPE removal timescale (12 hours), and t_{step} refers to the CAM4 timestep (30 minutes).

Apart from defining an air parcel spectrum at each initial starting model level, the above expression is similar to the mass flux closures used in other convective parameterizations. Convection occurs in response to the presence of CAPE. However, we have introduced an additional parameter AMP which is also intended scale with the degree of convective organization in the grid column. We assume that the presence of convective precipitation on the previous timestep generates sub-gridscale mesoscale circulations which increase the cloud base mass flux. The dependence of the AMP parameter on the lagged mean rainfall rate R_{mean} is identical to that used for the moist enthalpy width dk_m , except that we use different parameters. These parameters are given in Table 1. The dependence of AMP on R_{mean} is also shown in Figure 8.

A3. Updraft Parcel Mixing

Air parcels with positive CAPE are given an initial upward kinetic energy of 20 J/kg to overcome the local convective inhibition. Air parcels mix with the background atmosphere

490 using a buoyancy gradient formalism that is unchanged from the previous version of the
 491 model [Folkins, 2009]. The fractional entrainment (or detrainment) of mass associated
 492 with the movement of an updraft parcel from level $i - 1$ with buoyancy $b_p(i - 1)$, to level
 493 i with buoyancy $b_p(i)$ is given by

$$494 \quad \sigma = \frac{b_p(i) - b_p(i - 1)}{b_{mix}}. \quad (\text{A5})$$

495 The rate with which an updraft parcel mixes with the background atmosphere is inversely
 496 proportional to a buoyancy scale parameter b_{mix} . This formalism ensures that updraft
 497 parcels entrain ($\sigma > 0$) when their buoyancy increases, and detrain ($\sigma < 0$) when they
 498 encounter stable layers and lose buoyancy. Air parcels fully detrain into the background
 499 atmosphere when their buoyancy becomes negative.

500 Model simulations suggest that larger deep convective updrafts mix less with their
 501 environment than smaller shallow cumulus [Del Genio and Wu, 2010]. The b_{mix} parameter
 502 is therefore specified to be an increasing function of R_{mean} , using the same formalism
 503 used to calculate the moist enthalpy spectrum width dk_m . The parameters used in the
 504 expressions for b_{mix} are given in Table 1, and its dependence on R_{mean} shown in Figure
 505 8. As a result of the dependence of b_{mix} on rain rate, updraft parcels tend to have larger
 506 buoyancies, and detrain at higher altitudes, when rain rates are higher.

507 In order to determine the entrainment or detrainment of air at a particular model level,
 508 we calculate both a forward and a backward buoyancy gradient. Because the two buoy-
 509 ancy gradients may be of opposite sign, an air parcel may both entrain and detrain at
 510 a particular model level. Each model level will also contain an updraft parcel spectrum,
 511 with each parcel having different rates of entrainment and detrainment. Within the up-

512 draft parcel spectrum, the parcels with less buoyancy will have higher detrainment rates,
 513 and are preferentially removed from the updraft.

A4. Updraft Parcel Microphysics

514 We assume that each updraft parcel has a maximum liquid water loading $r_{l,max}$. This
 515 maximum condensate loading increases with the convective precipitation on the previous
 516 timestep, using the same procedure as used for dk_m , with the parameter values given in
 517 Table 1. This effect is intended to represent the ability of larger convective plumes with
 518 larger buoyancies and updraft velocities to retain more condensate. When the updraft
 519 parcel temperature is colder than a “freezing” temperature T_{freeze} equal to 253 K, we
 520 set $r_{l,max} = 0$. This represents the greater efficiency of precipitation formation when ice
 521 condensation nuclei are likely to be present.

A5. Fractional Conversion of Excess Condensate to Precipitation

522 Some fraction f_{precip} of the updraft condensate in excess of $r_{l,max}$ is converted to pre-
 523 cipitation. The remainder is assumed to detrain into the background atmosphere (except
 524 when the background atmosphere at that particular height is saturated, in which case
 525 $f_{precip} = 1$). The efficiency with which updraft condensate is converted to precipitation
 526 increases with rain rate. We again use the same sigmoidal formalism as used for dk_m ,
 527 with the parameters listed in Table 1.

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532 Precipitation Climatology Project.

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| Variable | R_{scale} | R_{half} | Min Value | Max value | Description |
|--------------|-------------|------------|-----------------------|-----------------------|-----------------------------------|
| AMP | 15 mm/day | 45 mm/day | 1 | 25 | parcel mass amplification factor |
| dk_m | 15 mm/day | 35 mm/day | 500 J/kg | 6000 J/kg | parcel enthalpy spectrum width |
| b_{mix} | 15 mm/day | 40 mm/day | 0.12 m/s ² | 0.18 m/s ² | mixing buoyancy scale |
| $r_{l,max}$ | 15 mm/day | 40 mm/day | 1 g/kg | 3 g/kg | updraft condensate maximum |
| f_{precip} | 10 mm/day | 15 mm/day | 0.3 | 0.7 | condensate precipitation fraction |

Table 1. Parameter values for the variables which are assumed to depend on the local degree of convective organization. For each variable, the four parameters listed here are used to calculate a sigmoidal value of the variable using Eqs. (1) and (2).

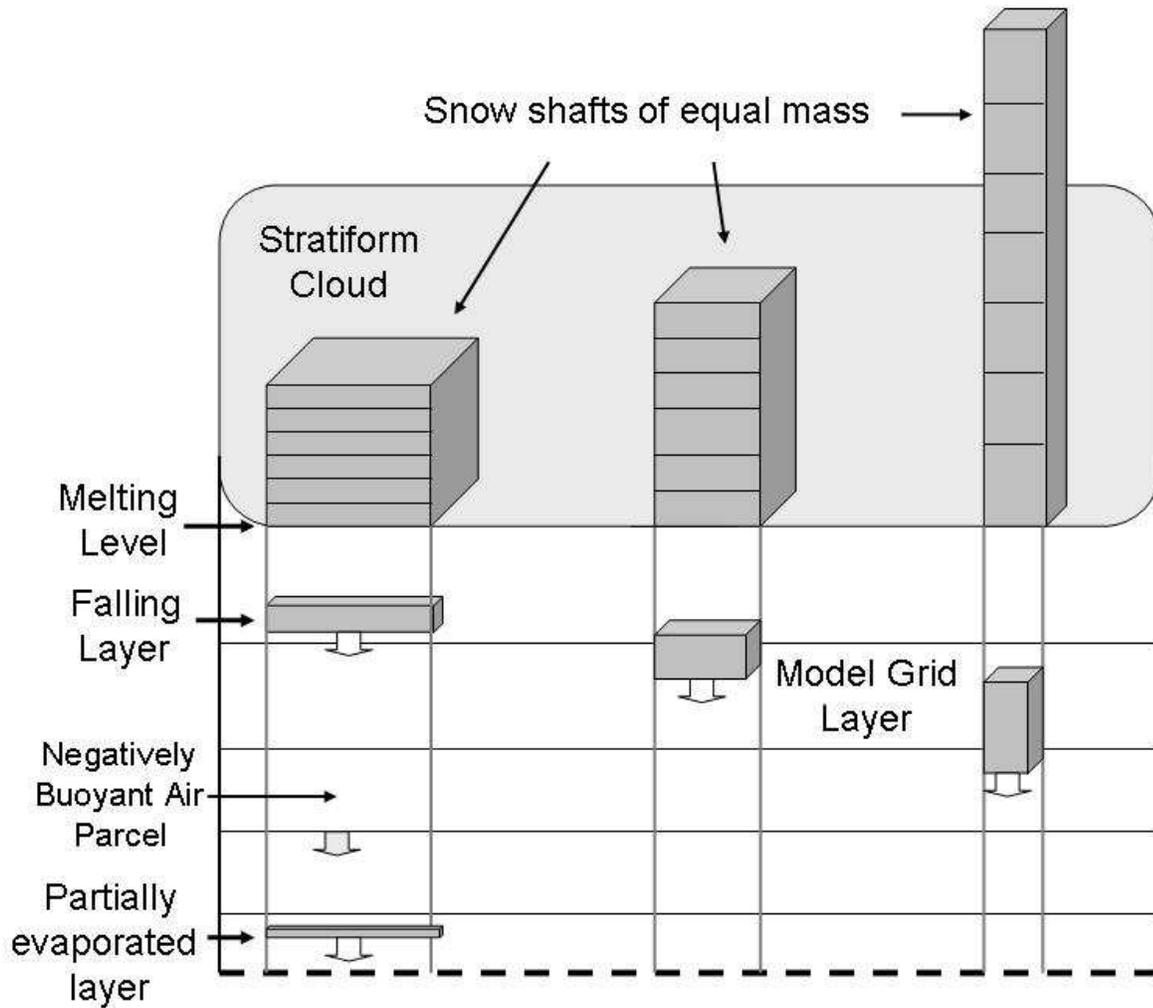


Figure 1. A conceptual diagram of the downdraft formalism of the convective parameterization.

See the text for explanation.

Gri-2.12.23/misc/users/clouds/folkins/BUBBLE/diurn/areas.gri (Wed May 8 11:28:24 2013)

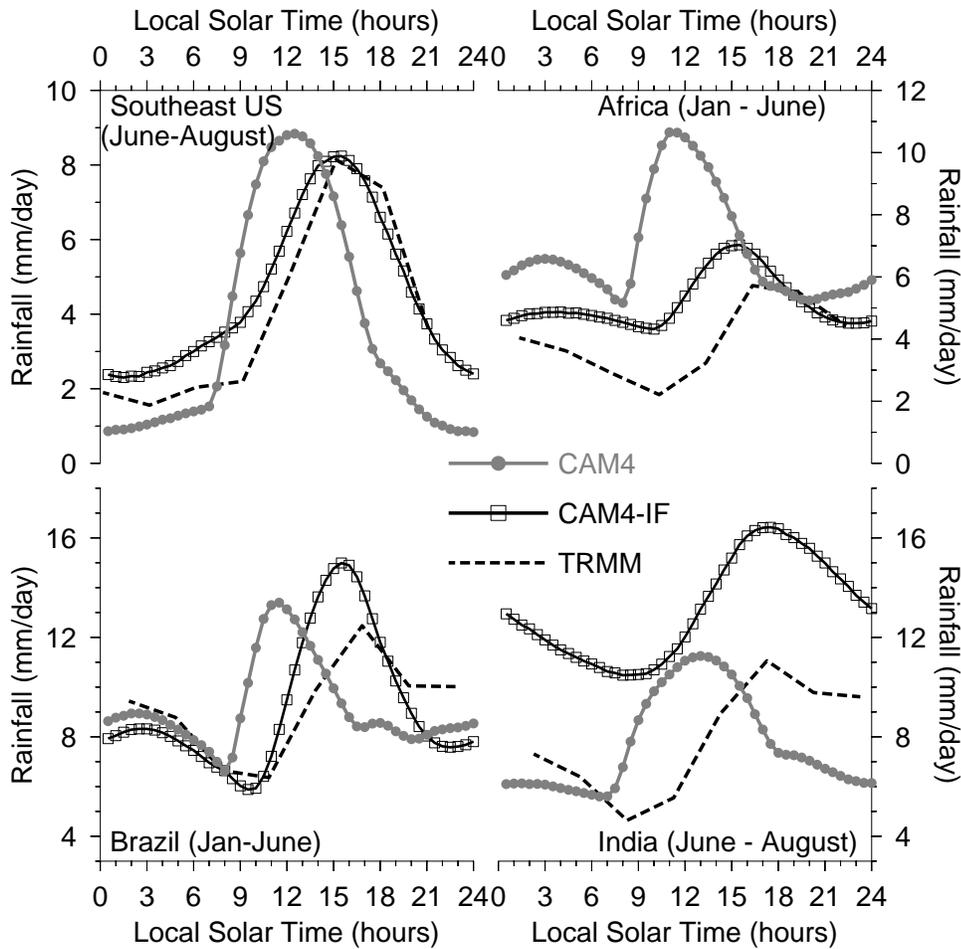


Figure 2. Each curve refers to the diurnal variation in rainfall of one of the four regions shown in Figure 3. Dashed curve: TRMM 3B42. Gray curves with solid circles: default CAM4 model. Black curves with open boxes: CAM4-IF model.

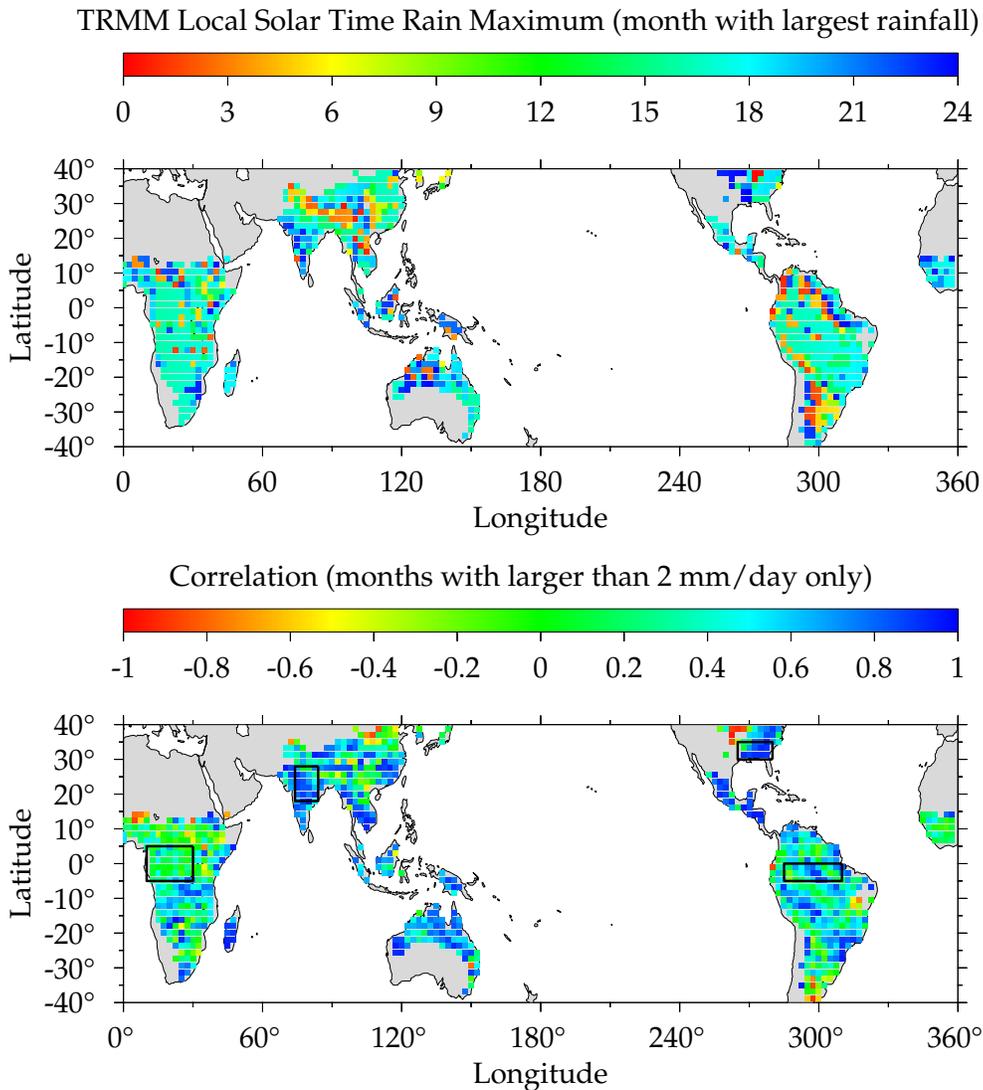


Figure 3. (upper) The local solar time of the diurnal peak in TRMM 3B42 rainfall, during the month with the largest mean rainfall. (lower) Correlation between the CAM4-IF and TRMM diurnal rainfall cycles, averaged over the months in which the mean rainfall rate of both datasets exceeds 2 mm/day.

Gri-2.12.23 /misc/users/clouds/folkins/BUBBLE/diurn/lst.gri (Wed May 8 11:28:26 2013)

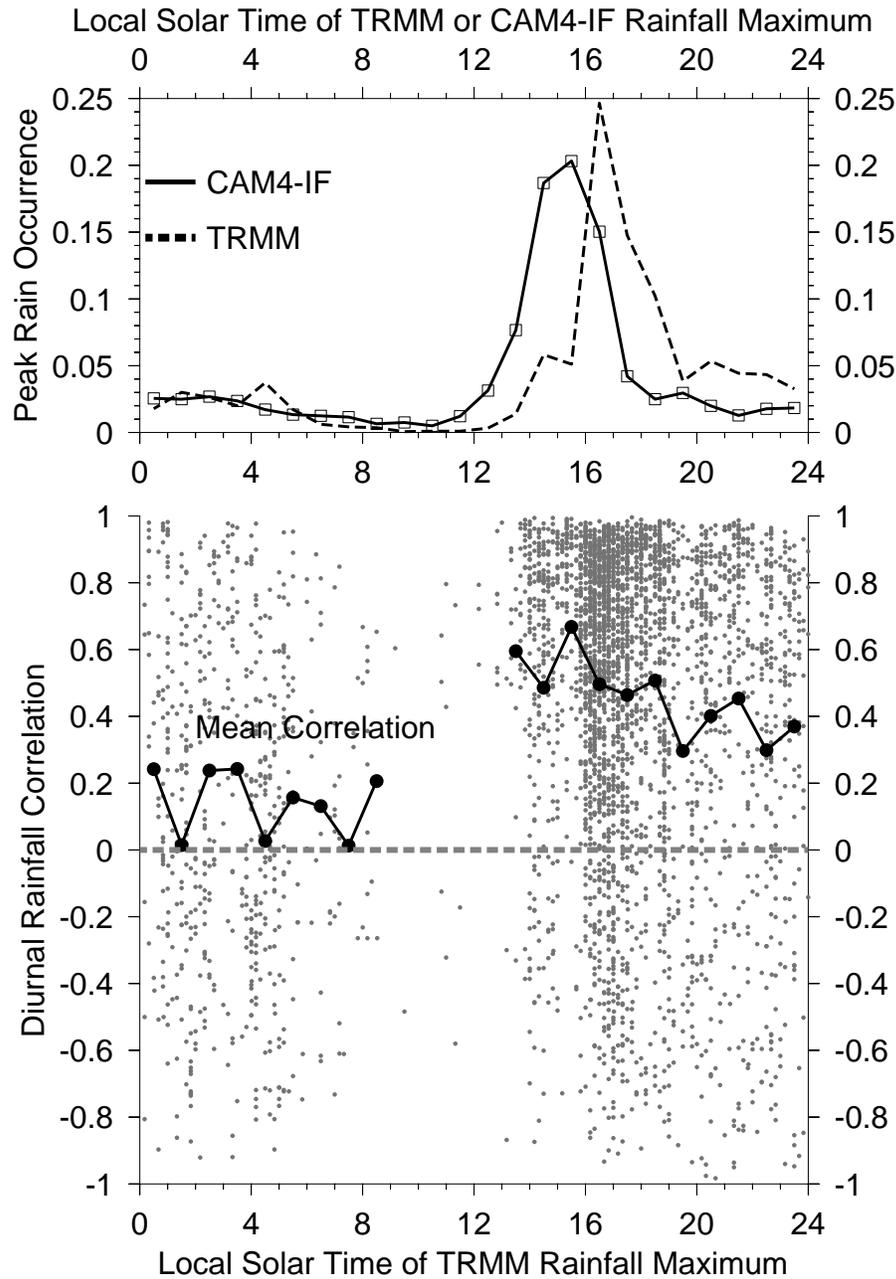


Figure 4. (upper) Dashed curve: the frequency of occurrence of the local time of peak TRMM 3B42 rainfall, for land grid cells where the monthly mean rain rate exceeds 2 mm/day. Solid curve: the frequency of occurrence of the local time of peak rainfall from the CAM4-IF model. (lower) Gray dots show the correlation between the local CAM4-IF and TRMM diurnal cycles, plotted against the local time of the TRMM rainfall peak. The solid curve was obtained by

binning the correlation coefficients in increments of one hour.
 D R A F T May 8, 2013, 11:28am

Gri-2.12.23 /misc/users/clouds/folkins/BUBBLE/diurn/cape.gri (Wed May 8 11:28:27 2013)

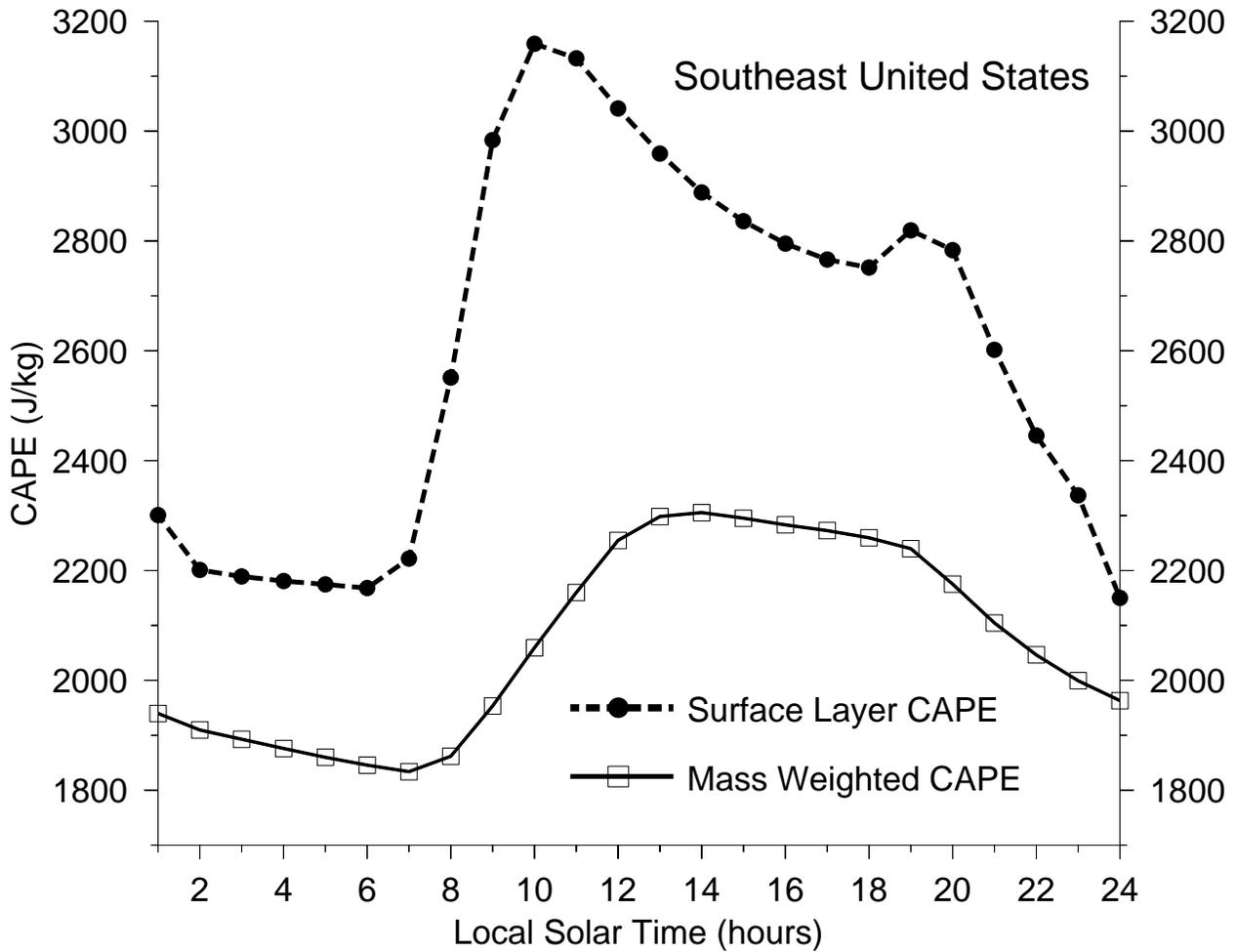


Figure 5. The diurnal variation of the CAPE of the surface layer (dashed) and the mass weighted CAPE of the lowest four model layers (solid), of the CAM4-IF model in the Southeast United States Region during July.

Gri-2.12.23 / misc/users/clouds/folkins/BUBBLE/diurn/r.mod.gri (Wed May 8 11:28:28 2013)

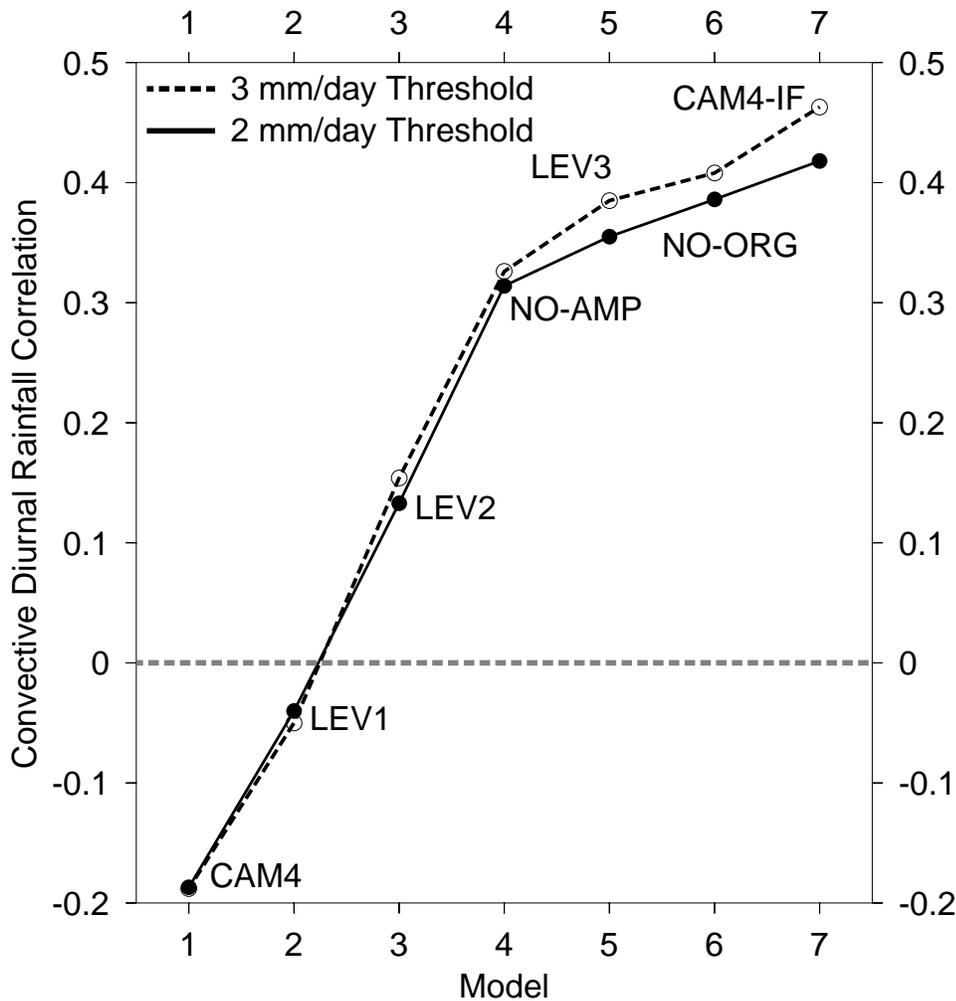


Figure 6. For each model simulation, we calculated the local correlation coefficient between the diurnal cycle in convective rainfall calculated by the model and the diurnal cycle calculated from the TRMM 3B42 dataset. A mean correlation coefficient was calculated by averaging over all land grid cells where the rainfall was likely to be convective. The solid line shows the dependence of the average correlation on the model simulation where we applied a rain threshold to each grid cell of 2 mm/day. The dashed curve used a rain threshold of 3 mm/day.

Gri-2.12.23 /misc/users/clouds/folkins/BUBBLE/diurn/r.gri (Wed May 8 11:28:29 2013)

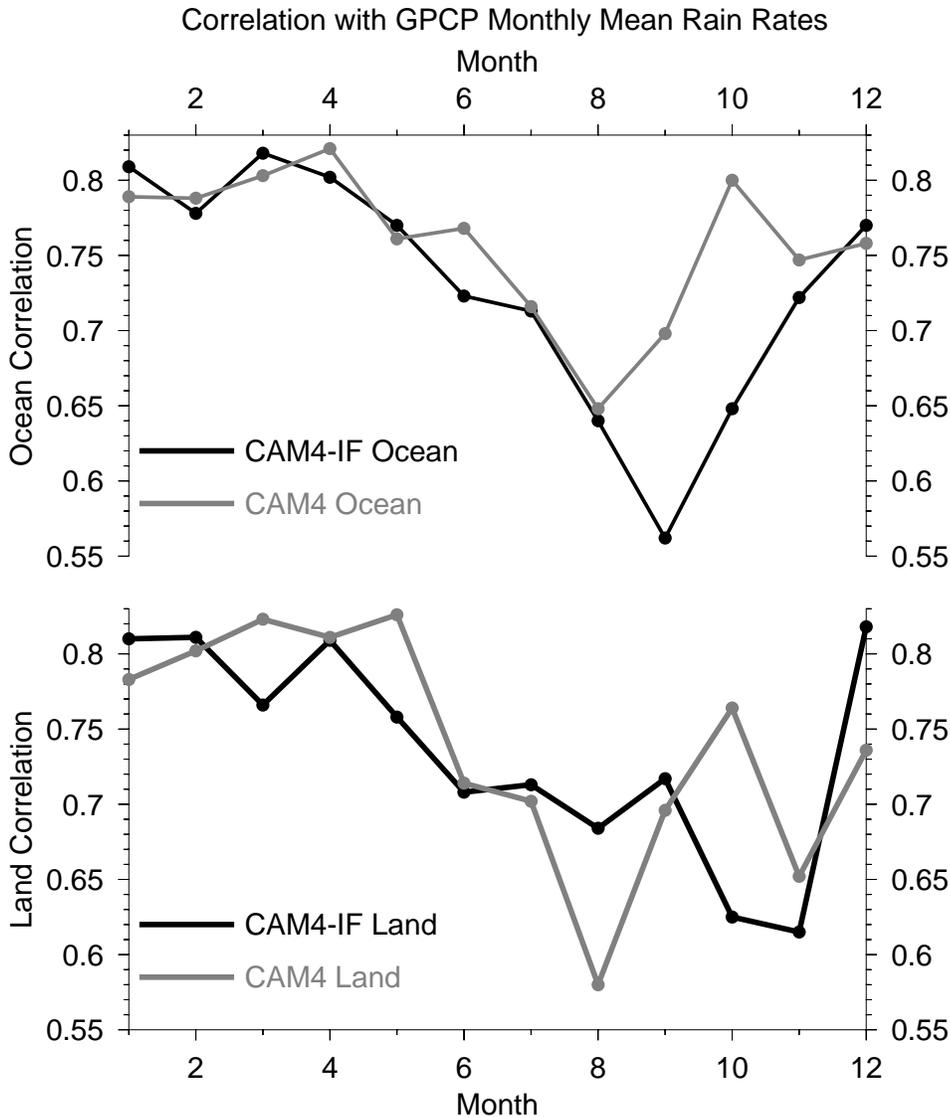


Figure 7. Three year runs of the CAM4 and CAM4-IF models were used to generate monthly mean rainfall rates. For each month, we calculated the overall correlation with monthly mean GPCP rain rates using grid cells at which the rain was likely to be convective. (upper) Seasonal variation of the correlation coefficient using ocean grid cells. (lower) Seasonal variation of the correlation coefficient using land grid cells.

Gri-2.12.23 /misc/users/clouds/folkins/BUBBLE/diurn/km.gri (Wed May 8 11:28:30 2013)

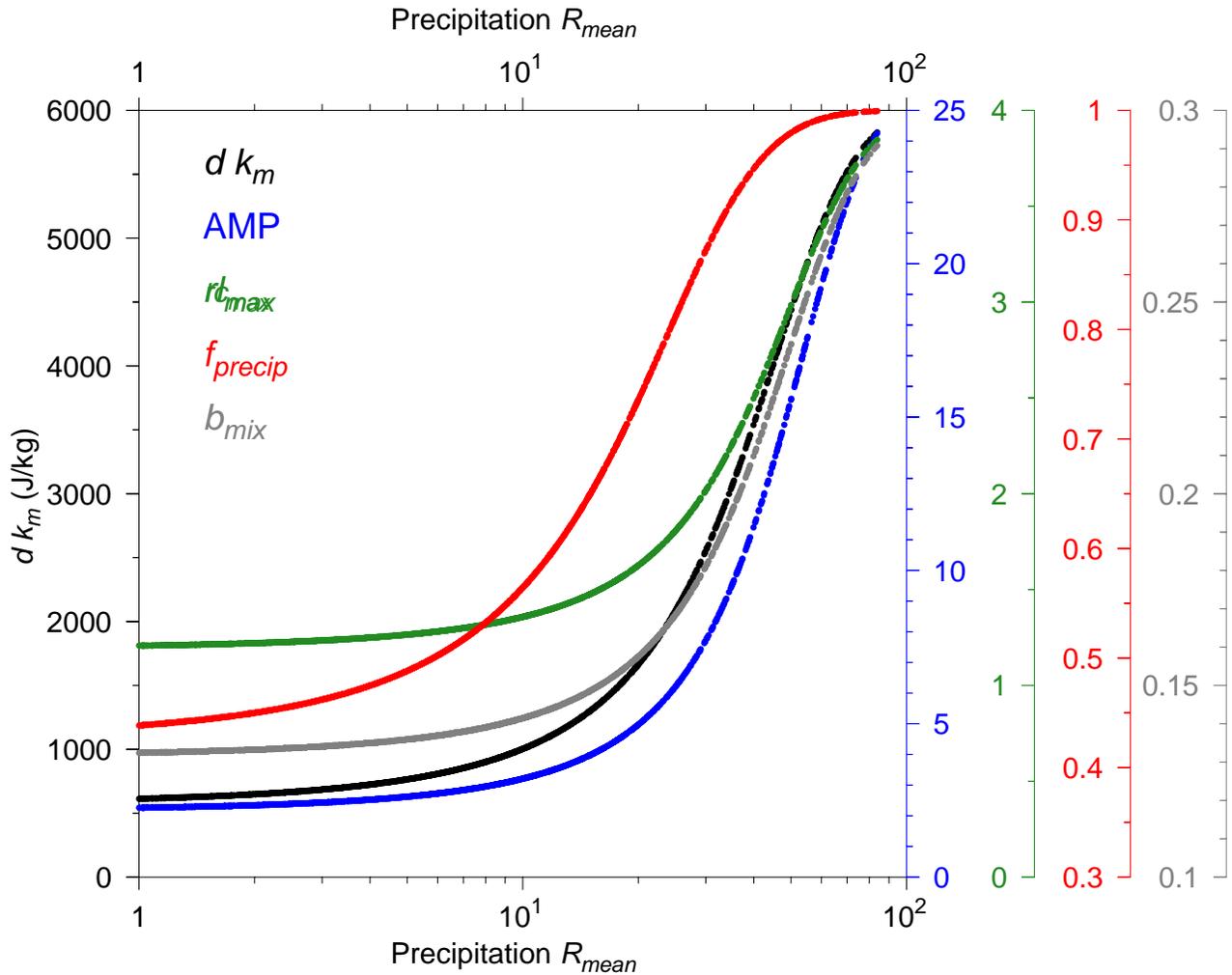


Figure 8. Each curve shows the sensitivity of a particular variable used in the convective parameterization to R_{mean} , roughly equal to the mean rainfall rate of a grid column over the previous two hours. The formulas used to calculate the sigmoidal curves are given in the Appendix. At low values of R_{mean} , the variables converge to the minimum value listed in Table 1. At large values of R_{mean} , the variables converge toward the sum of the minimum and maximum values listed in Table 1.