

## Review of logarithms

- We will discuss here natural logarithms, which are most commonly used in science.
- We will denote the logarithm of a number  $a$  as  $\log(a)$ , although you may also see  $\log_e(a)$  or  $\ln(a)$ .
- The logarithm of  $a$  is the number to which you have to raise  $e$  in order to get  $a$ .
- So if  $a = e^b$  then  $b = \log(a)$ .
- The symbol  $e$  is a mathematical constant approximately equal to 2.718.
- The exponential and logarithmic functions are inverses, so  $\log(e^b) = b$  and  $e^{\log(a)} = a$ .
- Here are some useful properties of natural logarithms
  1.  $\log(1) = 0$
  2.  $\log(c) < 0$  for  $c < 1$
  3.  $\log(c) > 0$  for  $c > 1$
  4.  $\log(e) = 1$

$$5. \log(c^d) = d\log(c)$$

$$6. \log(cd) = \log(c) + \log(d)$$

$$7. \log(c/d) = \log(c) - \log(d)$$

- Base ten (or common) logarithms and natural logarithms are related as

$$\log_e(a) = 2.303\log_{10}(a)$$