

$$\begin{array}{ccc} a & b & c \\ \text{If } d & e & f = 9, \text{ find } & 3a-5g & g & d \\ g & h & i & 3b-5h & h & e \\ & & & 3c-5i & i & f \end{array}$$

- A. -45
- B. 45
- C. -27
- D. 9
- E. 27
- F. -9

2. Which of the following are bases for  $\mathbb{R}^3$  ?

- (1) { (4, 2, 0), (0, 1, 2), (1, 3, -1) }
- (2) { (-1, 2, 3), (3, 3, 2) }
- (3) { (-1, 3, -5), (1, -2, 4), (2, 0, 4), (5, 1, 9) }

- A. (1) and (2)
- B. (1) only
- C. (2) and (3)
- D. None of them
- E. All three
- F. (2) only

3. Suppose  $A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 0 & 1 \\ 2 & 1 & 4 \end{bmatrix}$ . Which one of the following statements is true for  $A^{-1}$  ?

- A. None of the below is true.
- B. The second row is  $[1 \ 2 \ -1]$ .
- C. The first row is  $[2 \ 0 \ -1]$ .
- D. The third row is  $[-1 \ -1 \ 1]$ .
- E.  $A^{-1}$  does not exist.
- F. The second column is  $[0 \ 2 \ -1]^t$ .

4. Compute  $\begin{array}{cccc} -1 & 0 & -3 & 0 \\ 0 & -1 & 0 & -3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array}^{1001}$

- |    |   |    |   |
|----|---|----|---|
| A. | $\begin{array}{cccc} 1 & 0 & -3 & 0 \\ 0 & 1 & 0 & -3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array}$                  | B. | $\begin{array}{cccc} -1 & 0 & -3 & 0 \\ 0 & -1 & 0 & -3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array}$                    |
| C. | $\begin{array}{ccccc} -1 & 0 & -3^{1001} & 0 \\ 0 & -1 & 0 & -3^{1001} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array}$ | D. | $\begin{array}{ccccc} 1001 & 0 & -3003 & 0 \\ 0 & 1001 & 0 & -3003 \\ 0 & 0 & -1001 & 0 \\ 0 & 0 & 0 & -1001 \end{array}$ |
| E. | $\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array}$                    | F. | $\begin{array}{ccccc} -1001 & 0 & -3003 & 0 \\ 0 & -1001 & 0 & -3003 \\ 0 & 0 & 1001 & 0 \\ 0 & 0 & 0 & 1001 \end{array}$ |

5. If  $K = \{A \in M_{33} \mid A = -A^t\}$  is the subspace of anti-symmetric 3 by 3 matrices, then  $\dim K$  is:

- A. 3
- B. 2
- C. 6
- D. 9
- E. 4
- F. 0

6. Find all  $(a, b, c)$  so that  $\begin{matrix} a & 1 & b & b & 0 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & c \end{matrix}$  is in reduced row-echelon form.

- A.  $(0, 0, 1)$
- B.  $(1, 0, 0)$
- C.  $(1, 1, 1)$
- D.  $(0, 0, 0)$
- E.  $(1, 0, 0)$  and  $(0, 0, 1)$
- F.  $(1, 0, 0)$  and  $(0, 0, 0)$