

MATH 2600/STAT 2600, Theory of Interest

FALL 2014

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Homework Sheet 3

Due: Thursday 9th October: 11:30 AM

1. A loan of \$25,000 at $j_4 = 8\%$ is amortised with equal quarterly payments for 4 years.
 - (a) Calculate the monthly payments.
 - (b) Draw up a complete amortisation schedule for the loan.
2. Mrs. Quine takes out a 25-year mortgage for a loan of \$1,400,000 at $j_2 = 5\%$.
 - (a) Calculate the monthly payments required.
 - (b) After 5 years, the interest rate increases to $j_2 = 5.5\%$, calculate the new monthly payments if she wishes to keep the mortgage over 25 years.
 - (c) If instead, she wishes to keep the mortgage payments the same, when will she finish paying off the mortgage?
3. Mrs. Roberts borrows \$8,000 for one year at 7% simple interest. After 3 months, she repays \$3,000. How much does she need to pay 6 months after the start of the loan, to pay off the debt.
 - (a) If the loan is calculated using the U.S. rule?
 - (b) If the loan is calculated using the Merchant's rule?
4. Mr. Smith buys a cottage with a downpayment of \$50,000 and a 15-year mortgage for the remaining \$200,000 at $j_2 = 4\%$. There is a penalty of three times monthly interest on the outstanding balance for paying off the loan early. After 2 years, another company offers him a chance to refinance at $j_2 = 3.4\%$ for the remaining 13 years of the loan. Should he refinance?
5. Mr. and Mrs. Thorpe buys a house in the US. They need to borrow \$300,000 at $j_{12} = 5.2\%$, amortised over 25 years. There is also a financing fee of \$5,000. What is the APR for this loan?
6. A bank lends \$500,000 to Mrs. Underhill. The loan is paid back with monthly interest-only payments at $j_{12} = 6\%$, with the principal returned as a lump sum after 20 years. After 8 years, the bank sells the loan to a private investor, who wishes to achieve an annual effective yield of 5.4%.
 - (a) How much does the investor pay for the loan?
 - (b) If the bank wants to make an annual effective return of 5.3% on its investment, what annual effective yield would the buyer receive?

- (i) 6.21%
- (ii) 6.89%
- (iii) 7.24%
- (iv) 7.53%

7. Mrs. Vickers borrows \$300,000 to invest in the stock market. She has two options for repayment. She can either amortise the loan over 25 years at $j_{12} = 4\%$, or she can make interest only payments at $j_{12} = 4.4\%$ for 25 years, then pay off the balance with a lump sum payment at the end of the 25 years. What rate of return does she need on her investments to make the interest-only payments the better deal?

- (i) 4.80%
- (ii) 5.40%
- (iii) 5.76%
- (iv) 6.04%