

ACSC/STAT 4720, Life Contingencies II

Fall 2015

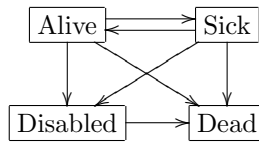
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Homework Sheet 1

Due: Friday 2nd October: 12:30 PM

Basic Questions

1. An insurance company is developing a new policy. The policy considers 4 states: Healthy, Sick, Disabled, and Dead. The transition diagram is shown below:



Which of the following sequences of transitions are possible? (Indicate which parts of the transition sequence are not possible if the sequence is not possible.)

- (i) Alive—Disabled—Sick—Dead
 - (ii) Alive—Disabled—Dead
 - (iii) Alive—Sick—Alive—Disabled
 - (iv) Alive—Sick—Dead—Disabled
2. Consider a permanent disability model with transition intensities

$$\begin{aligned}\mu_x^{01} &= 0.001 + 0.000003x \\ \mu_x^{02} &= 0.001 + 0.000001x^2 \\ \mu_x^{12} &= 0.003 + 0.000005x\end{aligned}$$

where State 0 is healthy, State 1 is permanently disabled and State 2 is dead. Calculate the probability that an individual aged 29 is alive but permanently disabled at age 56. [You may perform the integration numerically.]

3. Under a disability income model with transition intensities

$$\begin{aligned}\mu_x^{01} &= 0.001 \\ \mu_x^{10} &= 0.002 \\ \mu_x^{02} &= 0.001 \\ \mu_x^{12} &= 0.003\end{aligned}$$

calculate the probability that a healthy individual dies within the next 7 years. [State 0 is healthy, State 1 is sick and State 2 is dead.]

4. Under a disability income model with transition intensities

$$\begin{aligned}\mu_x^{01} &= 0.001 \\ \mu_x^{10} &= 0.002 \\ \mu_x^{02} &= 0.001 \\ \mu_x^{12} &= 0.003\end{aligned}$$

calculate the premium for a 5-year policy with premiums payable continuously while the life is in the healthy state, which pays benefits continuously at a rate of \$130,000 per year while the life is in the sick state, sold to a life in the healthy state. The interest rate is $\delta = 0.04$ [State 0 is healthy, State 1 is sick and State 2 is dead.]

[Hint: the probability that the life is healthy t years from the start of the policy is $0.1362e^{-0.0055616t} + 0.8638e^{-0.0014384t}$, and the probability that the life is sick t years from the start of the policy is $0.2426e^{-0.0014384t} - 0.2426e^{-0.0055616t}$.]

5. A whole life insurance policy can end either through death or withdrawal. The transition intensities are

$$\begin{aligned}\mu_x^{01} &= 0.001 + 0.000002x \\ \mu_x^{02} &= 0.002 + 0.000001x\end{aligned}$$

Calculate the probability that an individual aged 43 withdraws from the policy at any time before they die. [State 0 is healthy, State 1 is withdrawn and State 2 is dead.]

Standard Questions

6. An insurance company is developing a new model for transition intensities in a disability income model. Under these transition intensities it calculates

$$\begin{array}{lll}\bar{A}_{34}^{02} = 0.14 & \bar{A}_{44}^{02} = 0.19 & \bar{A}_{44}^{12} = 0.21 \\ \bar{a}_{34}^{00} = 22.07 & \bar{a}_{44}^{00} = 19.30 & \bar{a}_{44}^{10} = 0.11 \\ \bar{a}_{34}^{01} = 0.64 & \bar{a}_{44}^{01} = 0.43 & \bar{a}_{44}^{11} = 17.32 \\ {}_{10}p_{34}^{00} = 0.934 & {}_{10}p_{34}^{01} = 0.022 & \delta = 0.03\end{array}$$

Calculate the premium for a 10-year policy for a life aged 34, with continuous premiums payable while in the healthy state, which pays a continuous benefit while in the sick state, at a rate of \$80,000 per year, and pays a death benefit of \$280,000 immediately upon death.