

ACSC/STAT 4720, Life Contingencies II

Fall 2016

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Homework Sheet 5

Due: Friday 18th November: 12:30 PM

Basic Questions

1. An insurance company sells a 5-year annual life insurance policy to a life aged 29, for whom the lifetable below is appropriate.

| x | l_x | d_x |
|-----|----------|-------|
| 29 | 10000.00 | 0.88 |
| 30 | 9999.12 | 0.95 |
| 31 | 9998.17 | 1.03 |
| 32 | 9997.15 | 1.11 |
| 33 | 9996.04 | 1.21 |
| 34 | 9994.83 | 1.31 |

The annual gross premium is \$152. Initial expenses are \$90 plus 25% of the first premium. The death benefits are \$1,200,000. Renewal costs are 3% of each subsequent premium. The interest rate is $i = 0.03$

(a) Calculate the expected net cash-flows associated with this policy (assuming no reserve). [This is the profit vector for the policy.]

(b) Which of the following is the internal rate of return of the policy:

- (i) $i = 0.041241$
- (ii) $i = 0.049045$
- (iii) $i = 0.055031$
- (iv) $i = 0.061620$

2. An insurance company sells a 5-year annual life insurance policy to a life aged 44, for whom the lifetable below is appropriate.

| x | l_x | d_x |
|-----|----------|-------|
| 44 | 10000.00 | 7.25 |
| 45 | 9992.75 | 8.01 |
| 46 | 9984.74 | 8.85 |
| 47 | 9975.89 | 9.78 |
| 48 | 9966.11 | 10.81 |
| 49 | 9955.30 | 11.95 |

The annual gross premium is \$720. Initial expenses are \$130 plus 20% of the first premium. The death benefits are \$720,000. Renewal costs are 4% of each subsequent premium. The interest rate is $i = 0.03$. Reserves are calculated on the basis $i = 0.02$, with mortality following the table.

- (a) Calculate the reserves.
- (b) Calculate the profit signature.

- (c) Calculate the profit margin at a risk discount rate of $i = 0.06$.
3. For the policy in Question 2:
- (a) Calculate the reserves and profit signature for a general premium. [You may assume that P is such that the reserves are zero in Years 1 and 2.]
- (b) Calculate the premium that gives an internal rate of return of $i = 0.10$.
4. For a 5-year term insurance policy sold to a life aged 44, and actuary performs the following profit test without reserves:

| Year | Premium | Expenses | Interest | Expected Death Benefits | Pr_t |
|------|---------|----------|----------|-------------------------|----------|
| 0 | | 1500 | | | -1500 |
| 1 | 5900 | 0 | 177.00 | 4216.80 | 1860.20 |
| 2 | 5900 | 80 | 174.60 | 4806.66 | 1187.94 |
| 3 | 5900 | 80 | 174.60 | 5478.02 | 516.58 |
| 4 | 5900 | 80 | 174.60 | 6243.89 | -249.29 |
| 5 | 5900 | 80 | 174.60 | 7117.12 | -1122.52 |

Calculate the reserves needed to ensure that all cash flows are non-negative.

Standard Questions

5. A couple purchase a 5-year last survivor insurance policy. Annual Premiums of \$19,830 are payable while both are alive. If one life is dead, there are no premiums or benefits. If both lives die within the 5-year period, a benefit of \$1,000,000 is payable. The husband is 74 and the wife is 81. Their lifetables are given below. Assume both lives are independent.

| x | l_x | d_x | x | l_x | d_x |
|-----|----------|--------|-----|----------|---------|
| 74 | 10000.00 | 591.85 | 81 | 10000.00 | 1113.81 |
| 75 | 9408.15 | 628.62 | 82 | 8886.19 | 1114.43 |
| 76 | 8779.53 | 662.27 | 83 | 7771.76 | 1097.45 |
| 77 | 8117.26 | 691.27 | 84 | 6674.31 | 1061.21 |
| 78 | 7425.99 | 713.96 | 85 | 5613.10 | 1004.92 |
| 79 | 6712.03 | 728.54 | 86 | 4608.18 | 928.94 |

Initial expenses are \$3,000, and renewal expenses are \$80 at the start of each subsequent year while both are alive, and \$60 at the start of each year while only one is alive. The interest rate is $i = 0.04$. Use a profit test without reserves to determine the NPV of this policy at a risk discount rate of $i = 0.10$.