Kiyota OzekiOn~Melham's~Sum, Fibonacci Quart. $\bf 46/47~(2008/2009),~no.~2,~107–110.$

Abstract

The sum $L_1 \cdots L_{2m+1} \sum_{k=1}^n F_{2k}^{2m+1}$ was first considered by Melham. He noticed that for small m it could be expressed as a polynomial in F_{2n+1} . In this paper we give an explicit expansion for Melham's sum as a polynomial in F_{2n+1} .