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On Certain Combinations of Higher Powers of Fibonacci Numbers, Fibonacci Quart. 48 (2010), no. 3, 256–259.

Abstract

We present identities that we feel can be regarded as higher order analogues of the well-known identity $F_n^2 + F_{n+1}^2 = F_{2n+1}$. We give three theorems corresponding to the powers 4, 6, and 8. We also state two conjectures that give the form of similar identities that involve higher powers.