R. L. Ollerton
Catalan Numbers and Non-Intersecting Lattice Paths,
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Abstract

The convolution relation for Catalan numbers is used to show that they count certain non-intersecting lattice paths. Related uses and interpretations of the Catalan numbers in this context are also noted.