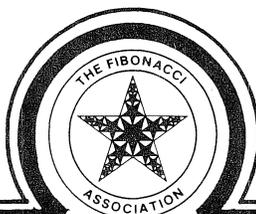


The Fibonacci Quarterly

THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION

VOLUME 19
NUMBER 1



FEBRUARY
1981

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The Fibonacci Quarterly

Founded in 1963 by Verner E. Hoggatt, Jr. (1921-1980),
Br. Alfred Brousseau, and I.D. Ruggles

*THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION
DEVOTED TO THE STUDY
OF INTEGERS WITH SPECIAL PROPERTIES*

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The principal purpose of *The Fibonacci Quarterly* is to serve as a focal point for widespread interest in the Fibonacci and related numbers, especially with respect to new results, research proposals, and challenging problems.

The *Quarterly* seeks articles that are intelligible yet stimulating to its readers, most of whom are university teachers and students. These articles should be lively and well motivated, with innovative ideas that develop enthusiasm for number sequences or the exploration of number facts.

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All back issues of *The Fibonacci Quarterly* are available in microfilm or hard copy format from UNIVERSITY MICROFILMS INTERNATIONAL, P.O. Box 1307, ANN ARBOR, MI 48106.