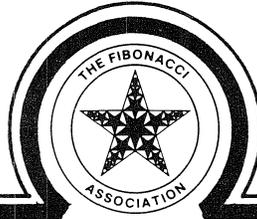


# The Fibonacci Quarterly

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# *The Fibonacci Quarterly*

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DEVOTED TO THE STUDY  
OF INTEGERS WITH SPECIAL PROPERTIES*

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The *Quarterly* seeks articles that are intelligible yet stimulating to its readers, most of whom are university teachers and students. These articles should be lively and well motivated, with innovative ideas that develop enthusiasm for number sequences or the exploration of number facts.

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