We see that the sequence  $a_n$  is defined by the rule  $a_{n+2} = k \cdot a_{n+1} + a_n$  for all  $n \ge 1$ . That is,  $a_n = F_n^{(k)}$ , and

$$\phi_k = \frac{x}{y} = \frac{F_{n+2}^{(k)} \cdot R_n + F_{n+1}^{(k)} \cdot R_{n+1}}{F_{n+1}^{(k)} \cdot R_n + F_n^{(k)} \cdot R_{n+1}} \approx \frac{F_{n+2}^{(k)}}{F_{n+1}^{(k)}}$$

This is the desired generalization of the geometric approximation in the introduction.

## ACKNOWLEDGMENT

The author appreciates the patience and advice of the anonymous referee whose comments and suggestions contributed largely to improving the form and presentation of this article.

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AMS Classification Number: 11B39

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## A MESSAGE OF GRATITUDE TO DR. STANLEY RABINOWITZ

The Editor, Editorial Board, and Board of Directors of The Fibonacci Association wish to express their deep gratitude to Dr. Stanley Rabinowitz for his excellent work as Editor of the Elementary Problems and Solutions section of *The Fibonacci Quarterly*. Our best wishes go with him as he retires from this position after nine years to devote full time to his publishing enterprise, MathPro Press.