The solution by William D. Jackson alluded to shows:

The number of Fibonacci numbers not greater than $\,N\,$ is the greatest integer less than

$$\frac{\log\left[\left(N+\frac{1}{2}\right)\sqrt{5}\right]}{\log\left(\frac{1+\sqrt{5}}{2}\right)} - 1$$

A FIBONACCI CROSSWORD PUZZLE

H.W. Gould West Virginia University

1		2		3			4		5	6			7
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ACROSS

- 2 A kind of number discovered by 17 Down of 22 Down while studying 50 Across.
- Series (French). 8
- 9 A river in Kansas and Missouri.
- 12 Smallest number into which each of two numbers will divide.
- 14 The smallest natural number (French).
- 15 One more than a perfect square.
- Occurrence of Fibonacci numbers in nature. 16
- $\lim_{n \to \infty} (1 + 1/n)^n$. 20

- 21 Device sometimes used to generate random numbers.
- 23 Combining form of "Chinese".
- 26 Letter used to denote a famous number sequence.
- Sign of differentiation. 27
- Brother of Abel. 28
- 29 Iron.
- 31 The numbers 1, 3, 4, 7, 11, ... are numbers.
- 32 Girl's name.
- 33 Measure of intelligence (they say).
- 35 Chemical element.
- $F_{n+1} = F_n + F_{n-1}$ is an example. Roman emperor. 36
- 39
- $(e^{x} + e^{-x})/2$. 41
- 43 Amateur.
- 44 Latin connective.
- Utilizes. 45
- 46 Square root of minus one.
- 47 If n is a natural number, then n+l is the natural number.
- Bitter Vetch. 49
- 50 Studied in 1202 AD by 2 Across.
- 51 Throws out.

DOWN

- 1 The first degree.
- 2 Battle.
- 3 Famous mathematician who wrote novels under the nom de plume John Taine.
- 4 Definite article (Arabic).
- 5 Cone-shaped.
- 6 A form of the copula.
- 7 Base of the decimal system.
- 10 Preposition.
- The function $x(1-x-x^2)^{-1}$ "the Fibonacci numbers.
- In fact, a Fibonacci number is the _____ of x^n in the power series expansion of $x(1 x x^2)^{-1}$.
- 16 Discovered a famous triangle named after him. Known earlier to the Chinese.
- 17 Another name of 2 Across.
- 18 One of the simplest ways to combine numbers.
- 19 The numbers 1, 1, 2, 3, 5, 8, ... form a _____.
- 22 A town in Italy.
- 24 An adjectival suffix.
- 25 A famous game whose theory is based on the binary system.
- 30 What one usually does with 13 Down in order to discover a relation.
- 34 City in ancient Sumer.
- 37 Chemical element discovered in Ytterby, Sweden.
- 38 Abbreviation for a trigonometrical function; counterpart of 41 Across.
- 39 Man's nickname.
- 40 A person who might live near 40°E. Long., 22°N. Lat.
- 42 To make a sharp sibilant sound.
- 43 Black substance obtained from coal.
- 45 An Indian of the Shoshonean tribes.
- 48 The Unknown Quantity.