

Counting (self-test)

How many?

1. 4 digit integers that start with 1 or 3 and are not a multiple of 10?
2. ways to arrange the letters $a, b, c, d, e, e, e, e, e$ so that no e follows another e ?
3. ways to put four Math books, two CS books and three Engineering books on a shelf so that books on the same topic are put together?
4. bit strings of length 6 that have at least 2 ones?
5. bit strings of length 8 that have exactly three ones, no two of which are consecutive?

Arrangements with repeated symbols:

If there are n objects of r different types with n_1 of the first type, n_2 of the second type, ... , and n_r of the r -th type, then there are

$$\frac{n!}{n_1!n_2!\cdots n_r!}$$

different arrangements of the given n objects.