

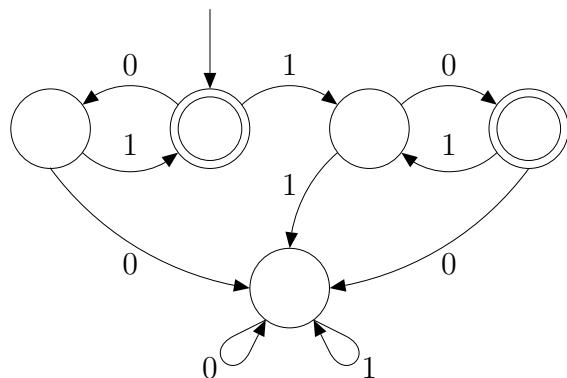
# MATH 2113 - Assignment 6

Due: Mar 4

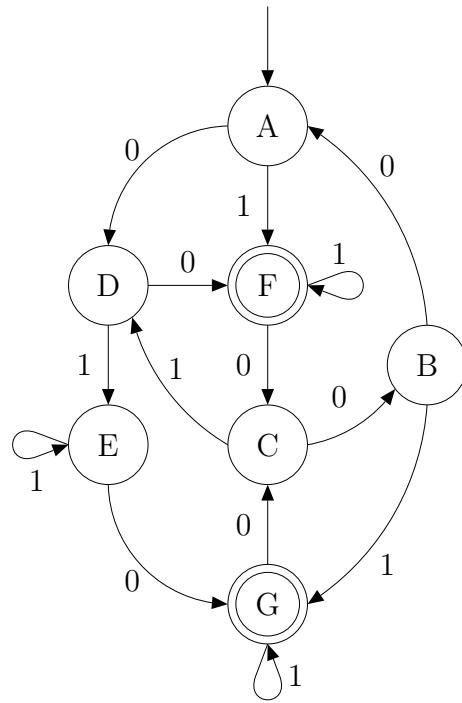
1. Let  $S$  be the set of states for a finite automaton and let  $\Sigma$  be the set of characters that it acts upon. We define the next state function  $N : S \times \Sigma \rightarrow S$ .
  - a) Under what conditions is  $N$  onto?
  - b) Under what conditions is  $N$  one to one?
  - c) Provide an example for both a) and b) where  $|S| = 4$ .
2. Find a finite automaton using the algorithm described in class which accepts the same set of strings generated by the regular expression:

$$0^*(1|11)0^*$$

3. Find a regular expression which accepts the same language as the following finite automaton:



4. Find the finite automaton with the fewest possible states which is equivalent to the following FA:



5. Find three "life" configurations which are periodic with  $p \geq 2$  different from the ones discussed in class.