

# MATH 3790 - Homework Set 1

Not to be handed in

September 17, 2003

1. Prove that  $\log_2 3$  is irrational.
2. Prove that  $7 \mid 2^{3n} - 1$ .
3. Find a closed form expression for the sum  $1 + 3 + 5 + \dots + (2n - 1)$  and prove that it is correct.
4. Prove that if  $a, b, c$  are integers and  $a \mid b$ ,  $b \mid c$  then  $a \mid c$ .
5. Prove that there are infinitely many primes.