

# ACSC/STAT 3720, Life Contingencies I

Winter 2015

Toby Kenney

Homework Sheet 5

Due: Friday 11th March: 12:30 PM

## Basic Questions

1. An insurance company offers a 10-year term policy with benefit \$800,000 payable at the end of the year of death. The premium for this policy for a select individual aged 37 for whom the lifetable in Table 1 is appropriate, is \$400, payable at the start of each year. If the current interest rate is  $i = 0.07$ , what is the probability that the present value of future loss for this policy exceeds \$150,000?
2. An insurance company offers a 5-year term policy with death benefit \$400,000 payable at the end of the year of death. If the interest rate is  $i = 0.06$ , calculate the annual premium for this policy for a select individual aged 36, using the lifetable in Table 1 and the equivalence principle.
3. The current interest rate is  $i = 0.04$ . An individual aged 42 to whom the ultimate part of the lifetable in Table 1 applies, wants to purchase a 15 year endowment insurance policy. The benefit of this policy should be \$500,000 either at the end of the year of death or at the end of 15 years. The initial costs to the insurance company are \$3,000 plus 10% of the first premium. Renewal costs are 4% of subsequent premiums. Calculate the Gross annual premiums for this policy. You calculate  $A_{42} = 0.154332$  and  $A_{57} = 0.261926$ .

## Standard Questions

4. A select individual aged 55, to whom the lifetable in Table 1 applies, wants to purchase a whole life insurance policy. She can afford to pay annual premiums of \$4,100 from now until age 80 (so she pays the last premium at age 79). The interest rate is  $i = 0.05$ , which gives  $A_{[55]} = 0.1801786$  and  $A_{[77]+3} = 0.457434$ . Using the equivalence principle to calculate net premiums, what is the largest death benefit that she can afford to purchase?
5. An individual aged 51 is paying premiums of \$200 a month for a whole life insurance policy which pays benefits at the end of the month of death. If the individual's mortality follows the ultimate part of Table 1, and the interest rate is  $i^{(12)} = 0.06$ , so that  $A_{51} = 0.112588$ , calculate the equivalent annual premiums (for a policy which pays benefits at the end of the year of death) using:
  - (a) Uniform distribution of deaths
  - (b) Woolhouse's formula
6. An insurance company provides a regular annual premium annuity contract to a select individual aged 44, using the lifetable in Table 1. The interest rate is  $i = 0.06$ . This gives that  $A_{[62]+3} = 0.218135$ ,  $A_{[72]+3} = 0.332028$  and  $A_{[44]} = 0.07872046$ . The individual will pay annual net premiums until age 65 (so the last premium will be at age 64). From age 65, they will receive an annuity of \$30,000 at the start of each year. This annuity is guaranteed for

10 years (regardless of whether the individual survives to age 65). What is the probability that the insurance company makes a net profit on this policy?

Table 1: Select lifetable to be used for questions on this assignment

$x$	$l_{[x]}$	$l_{[x]+1}$	$l_{[x]+2}$	$l_{[x]+3}$	$x$	$l_{[x]}$	$l_{[x]+1}$	$l_{[x]+2}$	$l_{[x]+3}$
25	9998.75	9997.65	9996.30	9994.66	74	8987.73	8932.10	8862.49	8775.52
26	9997.00	9995.83	9994.40	9992.66	75	8897.04	8836.71	8761.27	8667.10
27	9995.14	9993.90	9992.38	9990.52	76	8798.69	8733.34	8651.66	8549.78
28	9993.16	9991.84	9990.22	9988.24	77	8692.13	8621.41	8533.09	8423.00
29	9991.05	9989.65	9987.92	9985.80	78	8576.81	8500.36	8404.95	8286.16
30	9988.81	9987.30	9985.46	9983.18	79	8452.13	8369.60	8266.68	8138.66
31	9986.40	9984.80	9982.82	9980.38	80	8317.52	8228.53	8117.67	7979.93
32	9983.83	9982.11	9979.99	9977.37	81	8172.36	8076.57	7957.35	7809.41
33	9981.07	9979.23	9976.95	9974.13	82	8016.08	7913.13	7785.15	7626.56
34	9978.11	9976.13	9973.68	9970.64	83	7848.11	7737.67	7600.54	7430.89
35	9974.93	9972.79	9970.16	9966.88	84	7667.89	7549.66	7403.05	7221.99
36	9971.50	9969.20	9966.36	9962.82	85	7474.92	7348.64	7192.27	6999.51
37	9967.80	9965.33	9962.25	9958.44	86	7268.77	7134.21	6967.86	6763.22
38	9963.81	9961.14	9957.82	9953.69	87	7049.07	6906.07	6729.62	6513.04
39	9959.50	9956.61	9953.02	9948.55	88	6815.55	6664.05	6477.46	6249.02
40	9954.84	9951.71	9947.82	9942.98	89	6568.09	6408.10	6211.48	5971.42
41	9949.79	9946.41	9942.19	9936.94	90	6306.70	6138.35	5931.96	5680.73
42	9944.32	9940.66	9936.08	9930.38	91	6031.59	5855.15	5639.41	5377.67
43	9938.39	9934.41	9929.45	9923.26	92	5743.19	5559.08	5334.61	5063.27
44	9931.96	9927.64	9922.25	9915.52	93	5442.15	5250.97	5018.61	4738.86
45	9924.97	9920.28	9914.42	9907.10	94	5129.44	4931.97	4692.79	4406.12
46	9917.37	9912.28	9905.91	9897.94	95	4806.33	4603.54	4358.89	4067.08
47	9909.11	9903.58	9896.65	9887.98	96	4474.39	4267.51	4018.96	3724.10
48	9900.13	9894.11	9886.57	9877.13	97	4135.60	3926.04	3675.44	3379.91
49	9890.36	9883.80	9875.59	9865.30	98	3792.25	3581.66	3331.11	3037.57
50	9879.71	9872.57	9863.63	9852.42	99	3447.02	3237.23	2989.05	2700.39
51	9868.12	9860.34	9850.59	9838.38	100	3102.90	2895.94	2652.63	2371.88
52	9855.48	9847.01	9836.39	9823.08	101	2763.19	2561.21	2325.37	2055.64
53	9841.72	9832.48	9820.90	9806.39	102	2431.39	2236.61	2010.90	1755.27
54	9826.71	9816.64	9804.02	9788.18	103	2111.15	1925.80	1712.81	1474.18
55	9810.34	9799.37	9785.60	9768.33	104	1806.12	1632.34	1434.48	1215.44
56	9792.49	9780.52	9765.51	9746.67	105	1519.82	1359.55	1178.94	981.65
57	9773.03	9759.97	9743.60	9723.05	106	1255.46	1110.36	948.70	774.71
58	9751.79	9737.56	9719.69	9697.28	107	1015.81	887.14	745.58	595.71
59	9728.63	9713.10	9693.62	9669.17	108	802.96	691.49	570.56	444.87
60	9703.36	9686.43	9665.17	9638.51	109	618.23	524.17	423.71	321.41
61	9675.80	9657.33	9634.15	9605.07	110	462.04	385.00	304.13	223.65
62	9645.73	9625.59	9600.31	9568.61	111	333.80	272.80	210.00	149.10
63	9612.94	9590.98	9563.42	9528.85	112	231.99	185.53	138.71	94.62
64	9577.18	9553.24	9523.19	9485.52	113	154.19	120.34	87.07	56.74
65	9538.19	9512.09	9479.35	9438.30	114	97.30	73.90	51.50	31.84
66	9495.69	9467.25	9431.58	9386.86	115	57.78	42.55	28.41	16.52
67	9449.37	9418.39	9379.54	9330.85	116	31.92	22.69	14.43	7.81
68	9398.90	9365.17	9322.87	9269.88	117	16.15	11.04	6.63	3.30
69	9343.95	9307.23	9261.20	9203.55	118	7.34	4.79	2.69	1.21
70	9284.12	9244.18	9194.11	9131.43	119	2.90	1.79	0.93	0.37
71	9219.03	9175.59	9121.17	9053.07	120	0.95	0.55	0.26	0.09
72	9148.24	9101.03	9041.91	8967.97	121	0.23	0.13	0.05	0.01
73	9071.30	9020.03	8955.85	8875.63	122	0.03	0.02	0.01	0.00